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# High-intensity spatial-mode steerable frequency up-converter toward on-chip integration

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Integrated photonic devices are essential for on-chip optical communication, optical-electronic systems, and quantum information sciences. To develop a high-fidelity interface between photonics in various frequency domains without disturbing their quantum properties, nonlinear frequency conversion, typically steered with the quadratic ( $\chi^2$ ) process, should be considered. Furthermore, another degree of freedom in steering the spatial modes during the  $\chi^2$  process, with unprecedented mode intensity is proposed here by modulating the lithium niobate (LN) waveguide-based inter-mode quasi-phase-matching conditions with both temperature and wavelength parameters. Under high incident light intensities (25 and 27.8 dBm for the pump and the signal lights, respectively), mode conversion at the sum-frequency wavelength with sufficient high output power ( $-7 - 8$  dBm) among the  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes is realized automatically with characterized broad temperature ( $\Delta T \geq 8$  °C) and wavelength windows ( $\Delta \lambda \geq 1$  nm), avoiding the previous efforts in carefully preparing the signal or pump modes. The results prove that high-intensity spatial modes can be prepared at arbitrary transparent wavelength of the  $\chi^2$  media toward on-chip integration, which facilitates the development of chip-based communication and quantum information systems because spatial correlations can be applied to generate hyperentangled states and provide additional robustness in quantum error correction with the extended Hilbert space.

**Keywords:** integrated photonics; LN waveguide; sum-frequency generation; spatial-mode steering; on-chip integration

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## Introduction

Integrated photonic devices, consisting of diverse waveguides (optical circuits)<sup>1-2</sup>, microcavities<sup>3,4</sup>, modulators<sup>5-7</sup>, and laser sources<sup>8-10</sup>, are essential for next-generation optical communication<sup>11,12</sup>, optical-electronic systems<sup>13,14</sup>, and quantum information sciences in-

cluding quantum computation<sup>15,16</sup>, quantum signal processing<sup>17,18</sup>, and quantum sensing<sup>19,20</sup>. Photonics features, such as frequency, polarization, path, pulse shape, and orbital angular momentum (OAM), have been used for the functionality in space-division multiplexing<sup>21</sup>, polarization encoding<sup>22,23</sup>, spatial-temporal entanglement<sup>24</sup>,

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OAM multiplexing and de-multiplexing<sup>12,25,26</sup>, beam shifting and steering<sup>27,28</sup>, among others. Gathering these features matches the current trends in maximizing the link capacity for classical long-distance communications<sup>29</sup> and extending the Hilbert space of quantum systems<sup>30,31</sup>.

To develop a high-fidelity interface between photonics in various frequency domains without disturbing their quantum properties<sup>24,32</sup>, nonlinear frequency conversion, steered with quadratic ( $\chi^2$ ) processes, should be considered. These methods could be the classical second-harmonic generation (SHG)<sup>33,34</sup>, phase-matching-free SHG<sup>35</sup>, difference-frequency generation<sup>36</sup>, optical parametric oscillation<sup>37</sup>, and nonclassical spontaneous parametric down-conversion<sup>38,39</sup>. Meanwhile, accompanying spatial mode conversion was observed in the ferroelectric domain engineerable potassium titanyl phosphate (KTP) and lithium niobate (LN) crystals for quasi-phase matching (QPM) because of the inter-mode dispersion of the waveguide geometric<sup>40–43</sup>. This nontrivial process is promising in processing both the classical and quantum signals, such as selectively de-multiplexing the invisible multi-spatial mode signals toward the visible region<sup>44</sup> or preparing the high-dimension quantum states<sup>32</sup>. For inter-mode conversion, broadband lasers, or light sources with similar wavelengths<sup>42,45</sup> were applied, which rendered the prepared up-converted or down-converted spatial mode difficult to be discriminated because of their contiguous wavelengths<sup>41,45</sup>. This problem was determined using a tunable source as the fundamental wave (FW) in addition to the adjustment of the working temperature for phase matching<sup>41</sup>. However, the second harmonic (SH) wavelength of the spatial mode was uncontrollable with obvious shifting. By adjusting position of the FW inside a periodically poled LN (PPLN) waveguide to excite suitable FW modes<sup>40,47</sup>, evolution in the spatial mode of the SH wave was observed, which changed from  $TM_{01}$ ,  $TM_{10}$ , to  $TM_{00}$  within a short temperature range from 23 °C to 26 °C<sup>48</sup>. However, because the intensity of the generated space-mode was extremely weak under poor incident fundamental wave intensity (–13.5 dBm at 800 nm in ref.<sup>40</sup> and 7 dBm at 1066 nm in ref.<sup>46</sup>), detail adjustment to the incident light for rigorous mode-matching was required to selectively inspire the specific spatial mode for detection. Although spatial mode of the fundamental light can be easily prepared with a bulky spatial mode modulator<sup>44</sup>, these measures inevitably prohibit development of the spatial mode

steering device for on-chip integration with other fundamental elements, such as the microlasers<sup>49</sup> and fail to meet the rapid development in chip-based integrated optics.

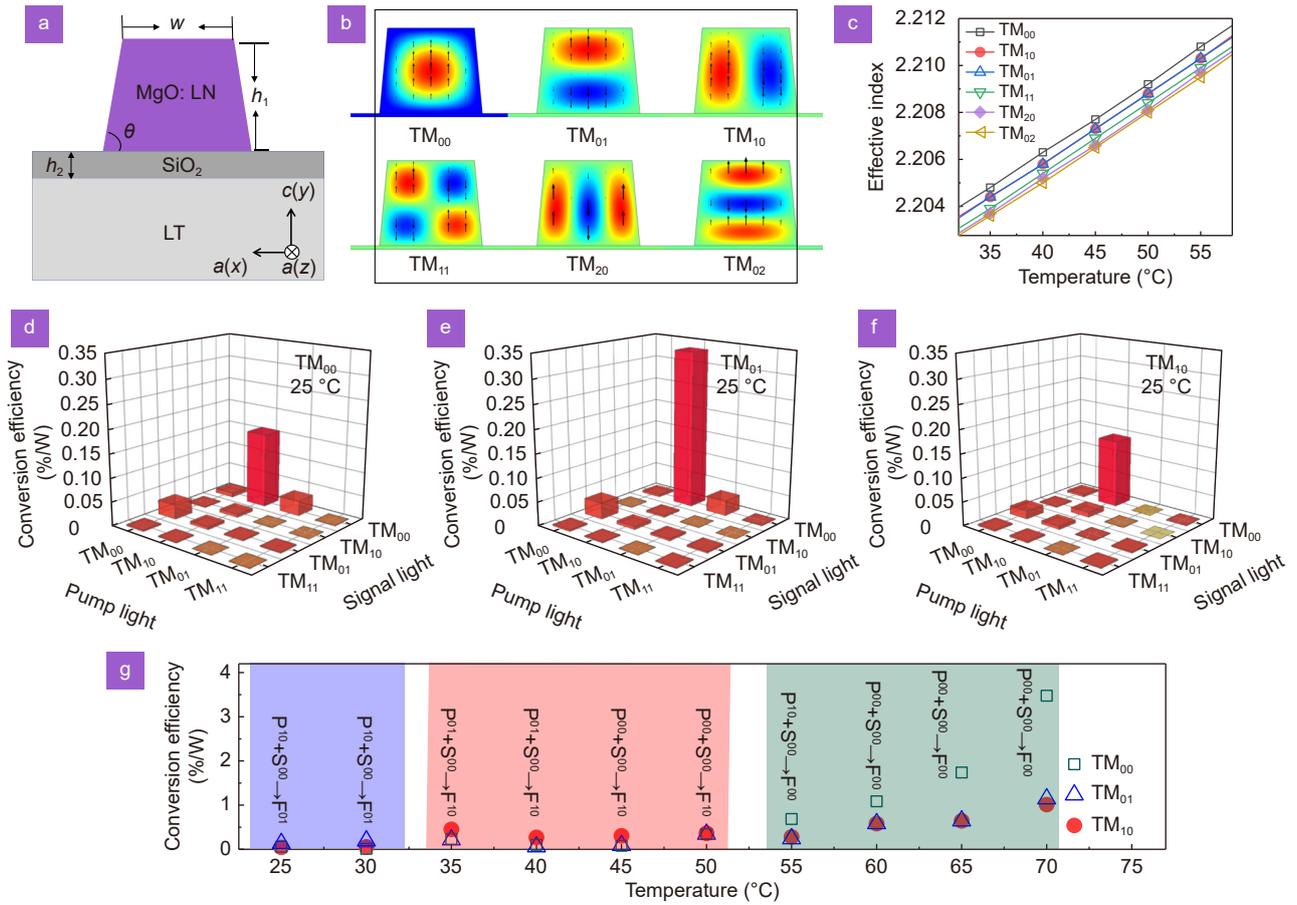
In addition to commonly up/down converting the spatial mode between the FW and SH<sup>41,47</sup>, the parametric process, dominated by three-wave mixing, is appealing, which provides an additional degree of freedom in selecting the mixing wavelength to satisfy the inter-mode QPM condition and making the target wavelength controllable without spectral drifting or broadening<sup>43–45</sup>. Furthermore, during a sum-frequency generation (SFG) process, the incident infrared signals could be selectively mode converted at the visible region, which can be easily detected and has ultra-low signal noise<sup>50</sup>.

In this paper, we demonstrate a high-intensity spatial-mode steering scheme during the SFG processes with a PPLN waveguide by separately manipulating the waveguide temperature and the wavelength of the mixing wave, which takes place under sufficient high incident light intensities (2~4 order of magnitudes higher than that in the previous reports<sup>40,46</sup>) without carefully adjusting incident lights or using the spatial light modulator<sup>40,44,48</sup>. Mode conversions at the SFG wavelength, among  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes, are realized at each characterized broad temperature ranges ( $\Delta T \geq 8$  °C) and wavelength ranges ( $\Delta \lambda \geq 1$  nm). The resulting mode intensities, un-reported in relevant literatures<sup>40–48</sup>, are within –7 – 8 dBm, which are sufficiently high for on-chip processing of both classical and quantum signals.

## Results and discussion

### Theoretical modeling

Among  $\chi^2$  optical materials, LN has received considerable attention in integrated optics because of its sufficiently high second nonlinear coefficient ( $d_{33} = 27$  pm/V<sup>51</sup>), engineerable ferroelectric domain for QPM, strong Pockels effect for electro-optical modulation<sup>5</sup>, and moderate third-order nonlinearity ( $1.6 \times 10^{-21}$  m<sup>2</sup>/V<sup>2</sup>) for acousto-optical modulation<sup>52</sup> or Raman processes<sup>53</sup>. In a few-mode PPLN waveguide with a poling period of  $\Lambda$ , nonlinear conversion among the signal ( $\lambda_S$ ), pump ( $\lambda_P$ ), and up-converted ( $\lambda_F$ ) waves is defined by the QPM condition, which is determined by the effective refractive indices  $n_S^{ml}$ ,  $n_P^{uv}$ , and  $n_F^{jk}$  of the waveguide. Here,  $jk$ ,  $uv$ , and  $ml$  define the numbers of the modal points of the



**Fig. 1 |** (a) Geometric of the prepared Z-cut PPMgLN waveguide with a poling period of 10.2  $\mu\text{m}$ , where  $w = 11.2 \mu\text{m}$ ,  $h_1 = 10.9 \mu\text{m}$ ,  $h_2 = 0.5 \mu\text{m}$ , and  $\theta = 75.1^\circ$ . (b) Characteristic mode profiles of the SFG light at 25  $^\circ\text{C}$ , described by the  $y$ -component of the electric field, where the arrows indicate directions of the electric field. (c) Effective indices for the TM modes of the SFG light, as the functions of the waveguide temperature. (d–f) Theoretical conversion efficiencies (CEs) by coupling among  $\text{TM}_{00}$ ,  $\text{TM}_{01}$ ,  $\text{TM}_{10}$ , and  $\text{TM}_{11}$  modes of the high-intensity pump and signal lights for the SFG lights with (d)  $\text{TM}_{00}$ . (e)  $\text{TM}_{01}$ , and (f)  $\text{TM}_{10}$  modes, respectively. (g) Predicted temperature conditions for producing the  $\text{TM}_{00}$  ( $F^{00}$ , cyan area),  $\text{TM}_{10}$  ( $F^{10}$ , red area), and  $\text{TM}_{01}$  ( $F^{01}$ , blue area) modes of the SFG light by comparing the maximum CE.

signal (S), pump (P), and SFG (F) lights along the horizontal and vertical directions. The effective index of the spatial modes can be linearly changed by the outer temperature ( $\sim 2.989 \times 10^{-4}/^\circ\text{C}$ ) because of the thermo-optical coefficient of the LN wafer (Fig. 1(c)) and enhanced by the waveguide geometric (Fig. 1(a)). Figure 1(b) lists the first six spatial modes of  $\lambda_F = 598.47 \text{ nm}$  at 25  $^\circ\text{C}$  (see the enumerated mode profiles for  $\lambda_S = 1552.6 \text{ nm}$  and  $\lambda_P = 973.85 \text{ nm}$  in Tables S2–S4 in the Supplementary information). We consider Type-0 QPM to use the maximum nonlinear coefficient  $d_{33}$  of the PPLN waveguide, in which the dominant TM mode with the electric field parallel to the waveguide height can be excited. With the calculated effective indices, the temperature-dependent inter-mode QPM equation can be described as follows:

$$\Delta(T) = \frac{n_F^{jk}(T)}{\lambda_F} - \frac{n_P^{uv}(T)}{\lambda_P} - \frac{n_S^{ml}(T)}{\lambda_S} - \frac{1}{\Lambda}. \quad (1)$$

Since the signal and pump lights are with high-intensity and approximately undepleted inside the waveguide, the conversion efficiency (CE) for spatial mode  $\lambda_F^{jk}$  at a given temperature is (see detailed derivation in the Supplementary information) as follows:

$$\eta_{\text{theo}}^{jk}(T) = \frac{8\pi^2 L^2 d_{\text{eff}}^2}{n_S^{ml} n_P^{uv} n_F^{jk} \epsilon_0 c \lambda_F^2} \Phi(x, y, T) \text{sinc}^2\left(\frac{\Delta k L}{2}\right), \quad (2)$$

where  $d_{\text{eff}}$  is the effective nonlinear coefficient of the LN crystal,  $\epsilon_0$  is the permittivity,  $c$  the speed of light, and  $\Delta k = 2\pi\Delta(T)$ , and  $\Phi(x, y, T)$  indicates the overlap integral among modes  $\lambda_S^{ml}$ ,  $\lambda_P^{uv}$ , and  $\lambda_F^{jk}$  at temperature  $T$  (see Supplementary information Eq. S6).

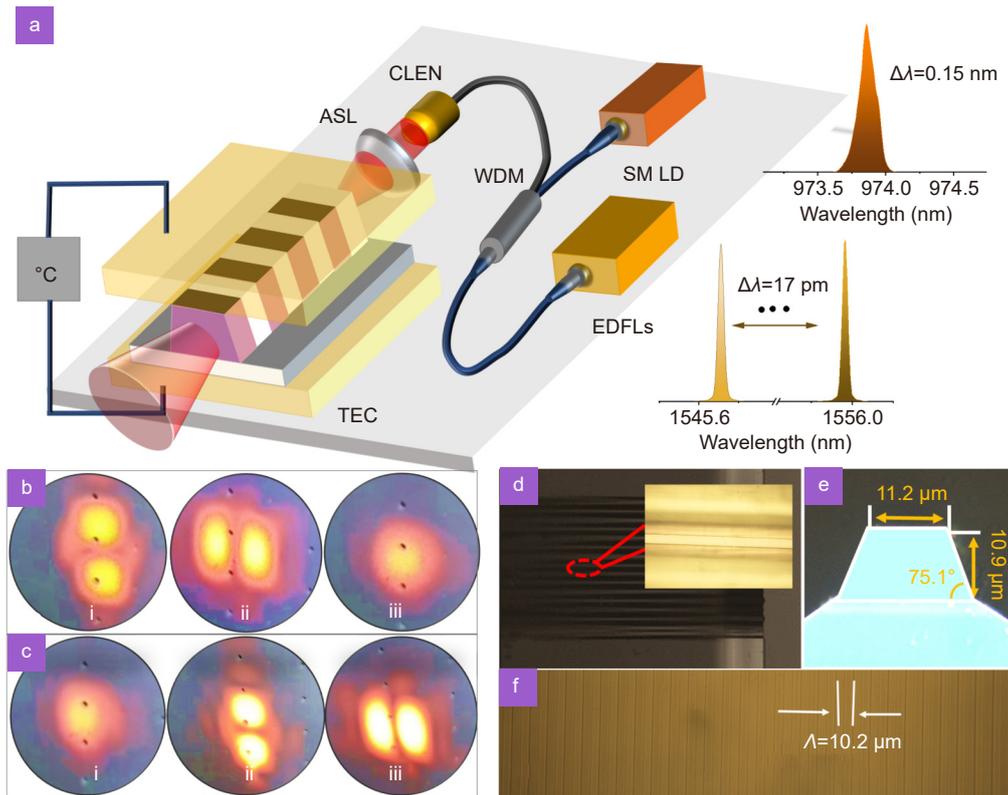
According to theoretical results (Fig. 1(d–f)), coupling among modes  $\text{TM}_{01}$ ,  $\text{TM}_{10}$ , and  $\text{TM}_{00}$  of the pump and signal and SFG lights dominates the spatial mode conversion process during frequency up-conversion. That is, at 25  $^\circ\text{C}$ , dominant processes  $\lambda_S^{00} + \lambda_P^{00} \rightarrow \lambda_F^{00}$ ,  $\lambda_S^{00} + \lambda_P^{01}$

$\rightarrow \lambda_F^{01}$  and  $\lambda_S^{00} + \lambda_P^{10} \rightarrow \lambda_F^{10}$  contribute for the potential  $TM_{00}$ ,  $TM_{01}$ , and  $TM_{10}$  modes with conversion efficiencies of 0.158%/W, 0.333%/W, and 0.143%/W, respectively. Thus, the resulting SFG mode under 25 °C is at  $TM_{01}$ , which automatically takes place under high incident pump and signal light intensities without specifically modulating spatial modes of the incident lights as the conventional manners. With the theoretical process, we could detail the spatial mode to be produced at a given temperature, and characteristic broad steerable temperature ranges for modes  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  are predicted (Fig. 1(g)).

### Experimental characterization

To verify theoretical prediction, we prepared a few-mode PPLN waveguide array consisting of seven waveguides with a length of 30 mm (Fig. 2(d)), which was diffusion-bonded on a lithium tantalate (LT) wafer with the assistance of a  $SiO_2$  layer (see Fig. S1 for the fabrication flow-

chart). The third waveguide, with well-protected cutting edge and lowest loss (0.29 dB/cm), was used throughout the experiment process (Fig. 2(e)). The ridge waveguide is characterized with a width of 11.2  $\mu m$  and height of 10.9  $\mu m$  to support at least 47, 11, and 50 eigenmodes at the pump, signal, and SFG wavelengths, respectively, at which three typical SFG modes ( $TM_{00}$ ,  $TM_{01}$ , and  $TM_{10}$ ), meeting the temperature controlled inter-mode QPM conditions are distinguished on a white broad (Fig. 2(b)). As with the designed poling period,  $\Lambda$  was measured to be 10.2  $\mu m$  using the microscopy image (Fig. 2(f)). We coupled signal light at the c-band from a tunable Erbium fiber-based master oscillator power-amplifier and pump light at 973.85 nm from a single-mode fiber-coupled diode laser into the ridge waveguide (Fig. S3), which was mounted inside a thermoelectric cooler (Fig. 2(a)). The pump and signal lights have maximum output powers of 25 dBm and 27.8 dBm respectively to implement an automatic spatial mode steering process, without specially



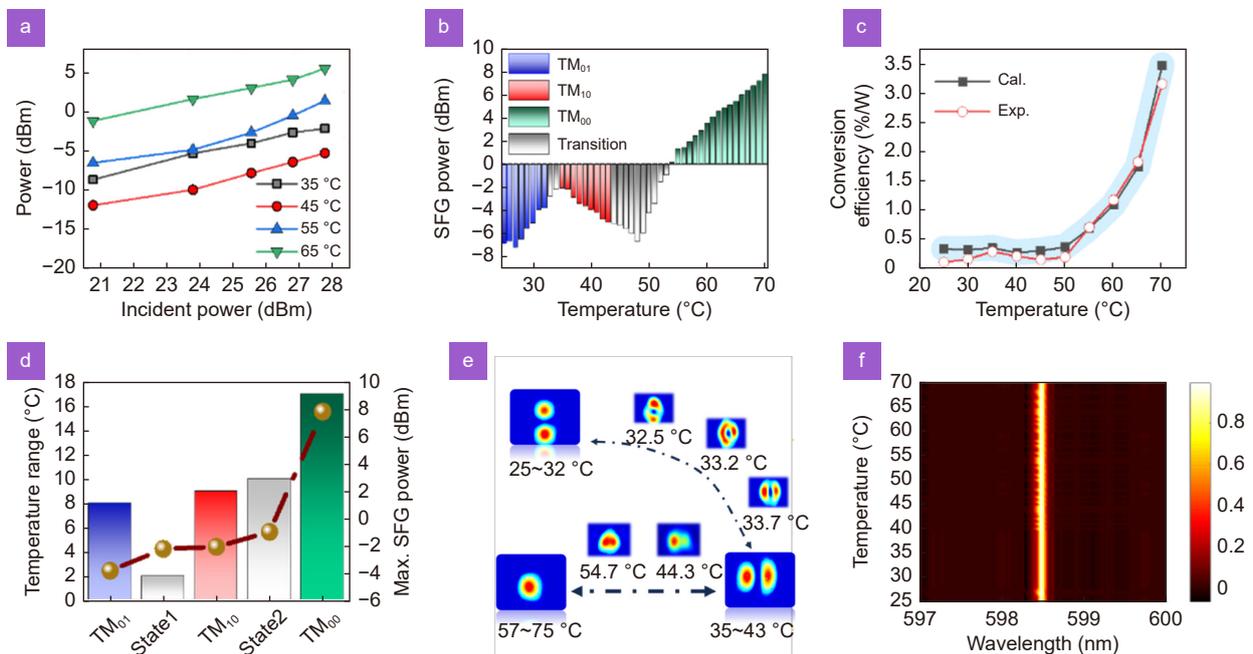
**Fig. 2 |** (a) Schematic of the temperature/wavelength-dependent spatial mode steerable SFG device. (b) In the temperature steering scheme, the detected up-conversion lights with (i)  $TM_{01}$ , (ii)  $TM_{10}$ , and (iii)  $TM_{00}$  modes at 30°C, 40°C, and 60°C, respectively, on a white broad. (c) In the wavelength steering scheme, the detected SFG lights with (i)  $TM_{00}$ , (ii)  $TM_{01}$ , and (iii)  $TM_{10}$  modes at 597.46, 597.99, and 598.41 nm, respectively, on a white broad. (d) Microscope image of the fabricated PPMgLN waveguide array on an LT wafer (Inset: detail profile of the third waveguide). (e) Cross-section view of the fifth waveguide selected in the experiments. (f) The fabricated polling structure with a period of 10.2  $\mu m$ . ED-FLs, Erbium-ion doped fiber laser system; SM LD, single-mode fiber-coupled diode laser; WDM, wavelength division multiplexer; CLEN, collimating lens; ASL, aspherical lens; TEC, thermoelectric cooler.

preparing the signal or pump modes in advance. Moreover, to avoid other potential spatial modes at the SFG wavelength caused by the broad bandwidth of the pump and signal waves<sup>45,47</sup>, their bandwidths are narrow and with values of 0.15 and 0.017 nm, respectively. Therefore, pure  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes are prepared stably at temperature ranges from 25 °C to 32 °C, 35 °C to 43 °C, and 54 °C to 70 °C, respectively (Fig. 2(b)). By tuning the signal wavelength from 1546 to 1556 nm, evolution in the spatial mode recurs and changes from  $TM_{00}$ ,  $TM_{01}$ , to  $TM_{10}$  (Fig. 2(c)). Both temperature- and wavelength-dependent steering methods are appealing in integrated optics through preparing target spatial modes with accessible wavelengths in the quantum or classical optical networks and overcoming the growing complexity of quantum information protocols.

On fixing the incident power of the pump light at 25 dBm, we measured the power curves of the SFG process at various temperatures from 25 °C to 70 °C (Fig. 3(a)) at which the signal wavelength was 1552.6 nm. The spatial mode did not change during each power scaling process at a given TEC temperature. Under an incident signal

power of 27.8 dBm, Fig. 3(b) depicts the maximum SFG power versus the working temperature. The regions for pure spatial mode are denoted with colors. Figure 3(c) displays the evolution of SFG efficiency (denoting by  $\eta_{exp} = 100 \cdot P_{SFG} / P_P / P_S$ ), which is consistent with the calculation result by denoting the maximum CE among  $F_{01}$ ,  $F_{10}$ , and  $F_{00}$  (Fig. 1(g)) as the theoretical efficiency  $\eta_{cal} = \max(\eta_{F10}, \eta_{F01}, \eta_{F10})$ . Controlling the waveguide temperature from 25 °C to 70 °C, the spatial mode begins with  $TM_{01}$  and subsequently changes from  $TM_{01}$  to  $TM_{10}$ , and  $TM_{10}$  to  $TM_{00}$  (Fig. 3(e)). Figure 3(d) depicts the width of temperature windows for  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes, with values of 8 °C, 9 °C, and 17 °C, respectively, which are sufficiently broad for a stable pure spatial mode generation. At each temperature window, the maximum SFG intensities are -3.82, -2.08, and 7.82 dBm, with corresponding conversion efficiencies of 0.21%/W, 0.29%/W, and 3.16%/W. The SFG spectrum is verified to be stabilizing at  $598.47 \pm 0.1$  nm when changing the waveguide temperature (Fig. 3(f)).

Between adjacent spatial modes, an obvious temperature window, covering a few Celsius degrees as the transition state, exists. This window can be attributed to the



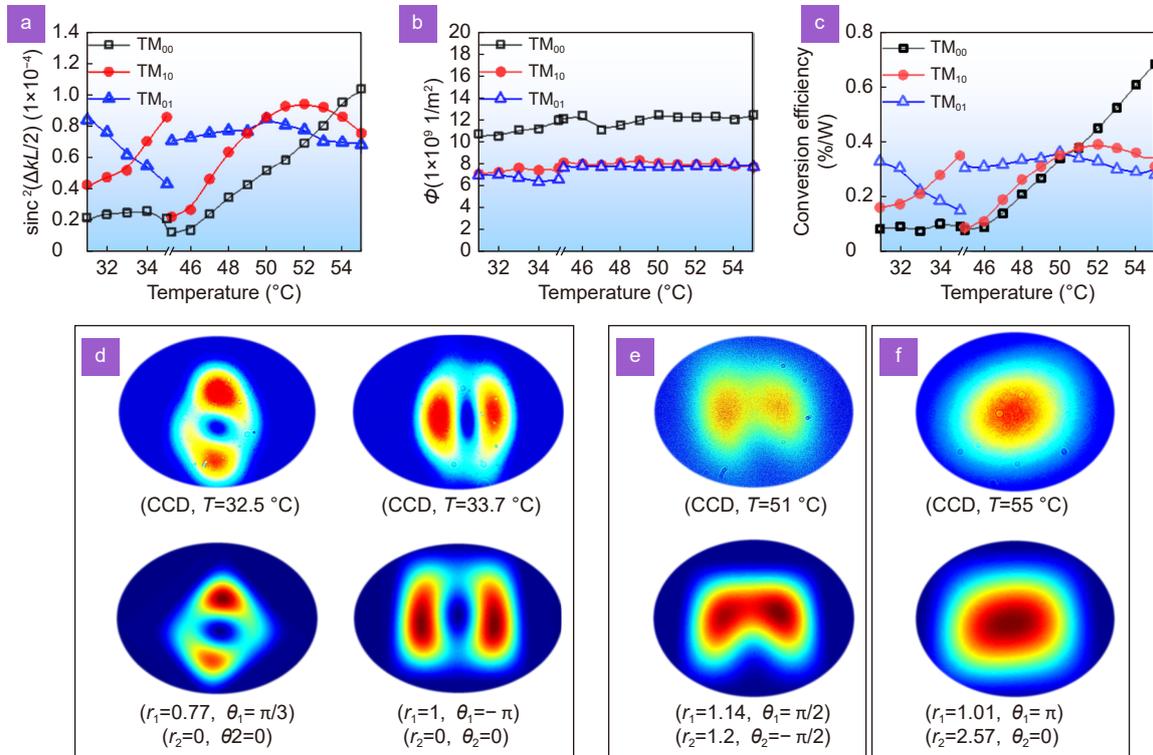
**Fig. 3 | Characterizing the temperature-dependent spatial mode steering scheme in the SFG waveguide.** (a) Power curves of the waveguide at typical temperatures of 35 °C, 45 °C, 55 °C, and 65 °C. (b) Evolution in SFG power under the maximum incident pump power of 27.8 dBm, in which the gray color denotes the regions without clear  $TM_{01}$ ,  $TM_{10}$ , or  $TM_{00}$  modes. (c) Experimental efficiency ( $\eta_{exp} = 100 \cdot P_F / P_P / P_S$ ) and theoretical efficiency ( $\eta_{cal} = \max(\eta_{F^{jk}}, \eta_{F^{jk}}, \eta_{F^{jk}})$ ) of the inter-mode up-conversion process. (d) Temperature windows for preparing mode  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$ , where state1 and state2 denote the transition process from  $TM_{10}$  to  $TM_{01}$  and  $TM_{01}$  to  $TM_{00}$ , respectively. (e) Mode profiles captured by the CCD camera to tell the exact modes during rising the waveguide temperature. (f) Evolutions in the SFG wavelength during the spatial mode steerable SFG process.

competition among the spatial modes with comparable conversion efficiencies. In the first transition state, mode rotation from  $TM_{01}$  to  $TM_{10}$  occurs (Fig. 4(d)), which was first observed in an SHG PPLN waveguide (within a small temperature range of  $\sim 2$  °C) and explained as the coupling between  $TM_{10}$  and  $TM_{01}$ <sup>48</sup>. However, in the second transition state, the rotated mode profile is distorted (Fig. 4(e)). According to the theoretical CE for modes  $TM_{00}$ ,  $TM_{01}$ , and  $TM_{10}$ , we could see CE for  $TM_{00}$  gradually increases and participates in the coupling between  $TM_{10}$  and  $TM_{01}$  with the increased waveguide temperature (Fig. 4(c)). Since the mode overlap integral  $\Phi(x, y, T)$  for  $TM_{00}$ ,  $TM_{01}$ , and  $TM_{10}$  is relatively stable (Fig. 4(b)), the resulting mixing mode patterns in transition states are originated by the temperature-dependent QPM efficiencies (denoted by  $\text{sinc}(\Delta kL/2)$ ) (Fig. 4(a)). We derive the mixing mode amplitude  $E_F^i(T)$  as follows:

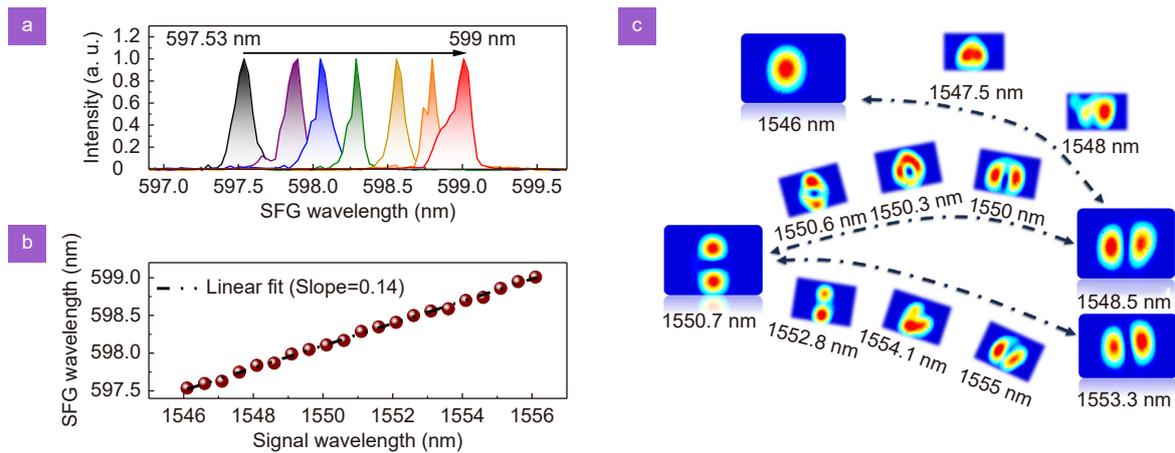
$$E_F^i(T) = \sum_{jk} A_F^{jk} E_F^{jk}(T), \quad (3)$$

where  $i$  denotes the  $i^{\text{th}}$  transition state, and  $jk$  the fundamental TM modes for the SFG light. Here  $jk = 00, 01,$  and  $10$  is selected and  $A_F^{jk}$  denotes the complex amp-

litudes for mode  $jk$ . Denoting  $A_F^{01} = 1$ , we obtain  $A_F^{10} = r_1 e^{i\theta_1}$  and  $A_F^{00} = r_2 e^{i\theta_2}$ , where ( $r_1 = \eta_{10}/\eta_{01}$ ,  $\theta_1$ ) and ( $r_2 = \eta_{00}/\eta_{01}$ ,  $\theta_2$ ) are the relative amplitudes and phase angles of  $A_F^{01}$  and  $A_F^{00}$  to  $A_F^{10}$ , respectively. In the first state, as the CE of  $TM_{00}$  is sufficiently small to be ignored, mixing mode patterns between  $TM_{10}$  and  $TM_{01}$  are computed and classified as the quasi- $TM_{01}$ , quasi- $TM_{10}$ , and highly coupling modes, in Fig. S4(a). The coupling modes occur at  $0.7 \leq r_1 \leq 3$  with  $0.8 \text{ rad} \leq \theta_1 \leq 2.2 \text{ rad}$  or  $-2.2 \text{ rad} \leq \theta_1 \leq -0.8 \text{ rad}$ . Therefore, the coupling mode patterns at 32.5 °C and 33.7 °C can be reproduced by setting ( $r_1, \theta_1$ ) as (0.77,  $\pi/3$ ) and (1,  $-\pi$ ) (Fig. 4(d)). In the second transition state, the mixing mode pattern is blurred because of the growing CE of  $TM_{00}$ . We address this three-mode coupling state by initializing the mode pattern under the two-mode coupling condition before sweeping parameters between  $r_2$  and  $\theta_2$  (Table S5). In addition to setting ( $r_1, \theta_1$ ) as (1.14,  $\pi/2$ ), ( $r_2, \theta_2$ ) = (1.2,  $-\pi/2$ ) is selected (Fig. 4(e)). In the third transition state,  $TM_{00}$  dominates the mixing mode, where the mode profile becomes convergent into a quasi  $TM_{00}$  mode with the increased waveguide temperature (Fig. 4(f)) and is insensitive to  $r_1, \theta_1,$  and  $\theta_2$  (Fig. S5).



**Fig. 4 | Transition states from two-mode coupling (first state), three-mode coupling (second state), to quasi  $TM_{00}$  mode (third state).** (a–c) Evolutions of the (a) inter-mode QPM efficiency ( $\text{sinc}(\Delta kL/2)$ ), (b) integral, and (c) conversion efficiency for  $TM_{00}$ ,  $TM_{10}$ , and  $TM_{01}$ , respectively. (d–f) Typical mixing mode pattern in the (d) first state, (e) second state, and (f) third state, respectively, where the upper picture is experimentally captured by a CCD camera, and the bottom picture is reproduced based on Eq. (3) with  $I = |E_F|^2$ .



**Fig. 5 | Characterizing the wavelength-dependent spatial mode steering scheme in the SFG waveguide.** (a, b) The changed SFG wavelength by increasing the signal wavelength from 1546 to 1556 nm: (a) spectral profiles, (b) fitted slope rate  $\Delta\lambda_p/\Delta\lambda_s = 0.14$ ; (c) at waveguide temperature of 25 °C, the evolution of the spatial mode from  $TM_{00}$  to  $TM_{10}$ ,  $TM_{10}$  to  $TM_{01}$ , and  $TM_{01}$  to  $TM_{10}$ .

Changing the signal wavelength from 1546 to 1556 nm, the SFG wavelength changes from 597.54 to 599 nm (Fig. 5(a)), where the slope rate is fit to be  $\Delta\lambda_p/\Delta\lambda_s = 0.14$ . Mode conversion occurs during red shifting the SFG wavelength (Fig. 5(c)). Theoretically, this method can be described by the inter-mode QPM condition (Eq. (1)), where the changed signal and pump wavelengths and the resulting effective indexes are considered:

$$\Delta(T, \lambda_p, \lambda_s) = \frac{n_F^{jk}(T, \lambda_F)}{\lambda_F} - \frac{n_P^{uv}(T, \lambda_p)}{\lambda_p} - \frac{n_S^{ml}(T, \lambda_s)}{\lambda_s} - \frac{1}{\Lambda}, \quad (4)$$

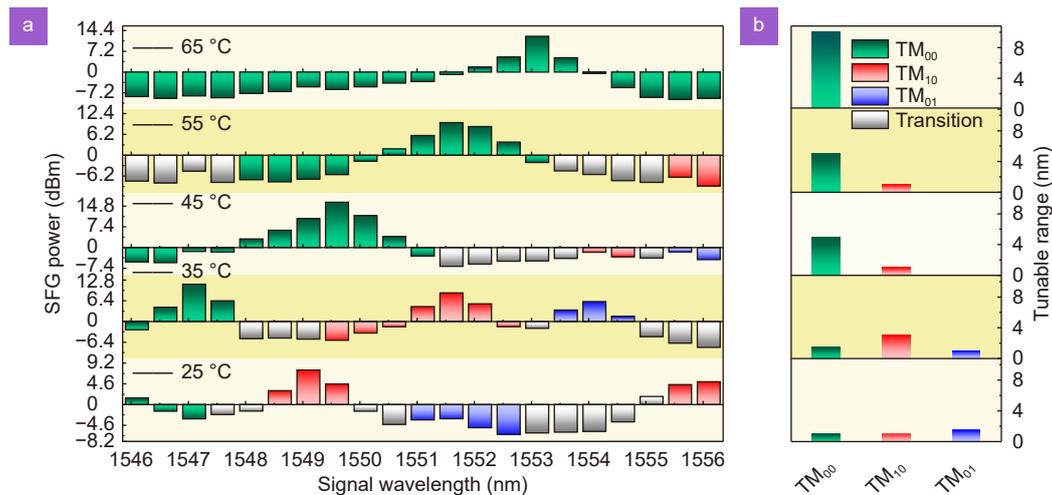
here,  $\lambda_F = 1/(1/\lambda_p + 1/\lambda_s)$ . Experimentally, Fig. 6(a) illustrates the measured SFG power during turning the signal wavelength at various waveguide temperatures (see Tables S6–S9 for the evolution processes of the spatial mode at 35 °C, 45 °C, 55 °C, and 65 °C, respectively), where the wavelength range for pure  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes is denoted. As with the temperature-dependent steering scheme, characterized broad wavelength windows to prepare the pure spatial modes by changing the signal wavelength are displayed (Fig. 6(b)). With the working temperature and incident mixing wavelengths, a 2D route map for preparing demanded spatial mode with up/down-conversion wavelength within the transparent window of the QPM  $\chi^2$  media can be determined.

## Conclusions

We have comprehensively demonstrated a high-intensity spatial-mode steerable frequency up-converter in both temperature and wavelength manipulating methods. Stable  $TM_{01}$ ,  $TM_{10}$ , and  $TM_{00}$  modes at the SFG

wavelength could be prepared automatically within a few-mode PPLN waveguide without prefabricating the spatial modes of the incident signal and pump lights by adjusting the incident combined lights or using a spatial light modulator. This result is appealing for on-chip integration with the microlasers such as distributed feedback laser (DFB)<sup>49</sup> or semiconductor optical amplifier<sup>54</sup>. The conversion processes can be theoretically explained by the competition among the SFG spatial modes under a high-intensity three wave mixing process described with the inter-mode QPM model, where a considerable broad temperature range with a width of approximately 8 °C and a waveband width of approximately 1 nm is displayed for the prepared spatial modes. The maximum mode switching speed is theoretically limited by the frequency-switching speed of the tunable pump or signal sources.

Moreover, because of the sufficiently high pump and signal light intensities, output power for the prepared up-converted spatial modes is within  $-7$  to 8 dBm (200  $\mu$ W to 6.3 mW), which has not been recorded in other literatures due to the poor fundamental wave intensity. This method is sufficiently high for on-chip preparation of the high-dimensional quantum information carriers in extending the Hilbert space and can be used in long-distance quantum communication and hyperentangled photon generation for increasing information capacity, improving the noise resistance, and making the quantum cryptographic schemes difficult to hack despite errors. Furthermore, the study has the potential in other functional devices including de-multiplexing the multi-mode signal by frequency conversion or encoding the target



**Fig. 6 |** (a) Evolution in SFG power at varied waveguide temperature under an incident pump and signal powers of 25.1 and 27.8 dBm, respectively, where characterized regions for the TM<sub>00</sub>, TM<sub>01</sub>, and TM<sub>10</sub> modes are denoted with cyan, red, and blue colors, respectively. (b) Wavelength windows for preparing the spatial mode during red shifting the SFG wavelength.

wavelength with characterized mode pattern<sup>55</sup>. Unlimited by the SFG scheme, the automatic spatial mode conversion process could also be implemented by differential frequency generation or optical parameter oscillation, which extends the desired wavelengths within transparent windows of the ferroelectric  $\chi^2$  media from ultra-violet to mid-infrared regions.

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## Author contributions

HZ Huang: Methodology, Investigation, Visualization, Writing—original draft; HX Chen: Device preparing, Data curation, Investigation, Writing—review & editing; HG Liu: Data curation, Writing—review & editing; Z Zhang, XK Feng, and JY Chen: Data curation, Visualization; HC Wu and J Deng: Formal analysis, Visualization; WG Liang: Supervision, Writing—review & editing; WX Lin: Conceptualization, Supervision.

## Competing interests

The authors declare no competing financial interests.

## Supplementary information

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