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# Pluggable multitask diffractive neural networks based on cascaded metasurfaces

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Optical neural networks have significant advantages in terms of power consumption, parallelism, and high computing speed, which has intrigued extensive attention in both academic and engineering communities. It has been considered as one of the powerful tools in promoting the fields of imaging processing and object recognition. However, the existing optical system architecture cannot be reconstructed to the realization of multi-functional artificial intelligence systems simultaneously. To push the development of this issue, we propose the pluggable diffractive neural networks (P-DNN), a general paradigm resorting to the cascaded metasurfaces, which can be applied to recognize various tasks by switching internal plug-ins. As the proof-of-principle, the recognition functions of six types of handwritten digits and six types of fashions are numerical simulated and experimental demonstrated at near-infrared regimes. Encouragingly, the proposed paradigm not only improves the flexibility of the optical neural networks but paves the new route for achieving high-speed, low-power and versatile artificial intelligence systems.

Keywords: optical neural networks; diffractive deep neural networks; cascaded metasurfaces

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# Introduction

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Deep learning is a form of machine learning that attempts to imitate the principles of the human brain for data interpretation. It has been applied to many specific tasks, including image classification<sup>1,2</sup>, image encryption<sup>3</sup>, intelligent photonic devices<sup>4,5</sup>, speech recognition<sup>6,7</sup>, and language translation<sup>8</sup>. However, deep learning is a data-driven algorithm that requires frequent reading and writing of large amounts of data using existing electronic computers. The calculation abilities of electronic computers are limited by the von Neumann architecture, which stores data and programs separately<sup>9</sup>. The bottleneck of computing performance caused by the mismatch between data reading and processing speed and the huge energy consumption caused by frequent data reading and writing have become blocks to the further development of artificial intelligence.

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In the last several decades, optical neural networks (ONNs)<sup>10-18</sup> have provided a solution by exploiting the unique properties of light and possess the advantages of high speed, high parallelism, and low energy consumption. Recently, deep neural networks have been implemented in optical systems using diffractive optical elements and validated in imaging processing and object recognition. The terahertz diffractive deep neural networks (D<sup>2</sup>NN) fabricated by 3D printing is the landmark example for ONNs<sup>19</sup>. Each unit structure of D<sup>2</sup>NN is regarded as a neuron, and the interconnections of neurons between layers are realized by diffraction of light. Metasurfaces, composed of subwavelength elements, are a novel type of two-dimensional planar structures, which provide promising platform for ultrathin flat optics compared to traditional diffractive optical elements<sup>20,21</sup>. The amplitude and phase of light can be controlled simultaneously by changing the size, arrangement and shape of meta-atoms inside the metasurface. The realization of D<sup>2</sup>NN with metasurfaces is helpful to realize miniaturized and multifunctional intelligent integrated devices<sup>22</sup>.

Currently, D<sup>2</sup>NN has been widely studied for various tasks, including broadband pulse shaping<sup>23</sup>, optical logic gate operation<sup>24</sup>, and OAM beam multiplexing and demultiplexing<sup>25,26</sup> among others<sup>27-29</sup>. In addition, some D<sup>2</sup>NNs with improved structures have been applied to wider fields, such as the multi-view D2NN array scheme for 3D object recognition<sup>30</sup>, where each D<sup>2</sup>NN corresponds to a 3D object view, ensemble learning of D<sup>2</sup>NN<sup>31</sup>, which introduces passive filters in space or Fourier space to preprocess input information and achieve higher-precision image classification, and Fourier-space D<sup>2</sup>NN<sup>32</sup>, which places the diffractive layer on the Fourier plane of the optical system to achieve all-optical saliency detection. However, once these architectures are trained and fabricated, they cannot be changed. If extra tasks need to be achieved, the parameters of the entire network have to be retrained. This process consumes a lot of computing resources to optimize the network parameters. Although there have been some studies on the reconfigurability problem of D<sup>2</sup>NN, such as programmable electromagnetic metasurface<sup>33</sup>, optoelectronic fusion computing architecture<sup>34</sup>, hardware-software co-design architecture<sup>35</sup>, on-chip polarization multiplexed diffractive neural networks. These methods introduced additional energy consumption and required complex experimental setups. Recently, the on-chip polarization multiplexing neural network has been proposed to achieve multitasking in

the visible light band<sup>36</sup>. However, this approach has limited performance with a single-layer metasurface.

Here, we proposed the pluggable diffractive neural networks (P-DNN), which can realize the switching of various recognition tasks such as handwritten digits and fashions by switching the pluggable components in the network. It improves the flexibility of network design while effectively reducing the consumption of computing resources and training time. We designed two-layer cascaded metasurfaces<sup>37</sup> to demonstrate the capabilities of P-DNN by using handwritten digits and fashions as input, respectively. Considering the experimental feasibility, the phase-only metasurfaces were used for verification. The experimental classification accuracies of handwritten digits and fashions classification tasks exceed 91.3% and 90.0%, while similar classification accuracies (91.8% and 90.2%) are obtained in P-DNN experimental verification. P-DNN is a general model for various classification tasks and provides an alternative for reconfigurability problems of D<sup>2</sup>NN. In addition, P-DNN can be used as an integrated component of artificial intelligence systems with different functions to provide low-energy, high-speed computing for specific tasks in the future, such as microscopy imaging, and autonomous driving assistance.

# Results and discussion

The framework of the proposed P-DNN can be used to recognize various types of datasets such as handwritten digits and fashions, as shown in Fig. 1. We took the object to be classified as input, phase-encoding neurons as hidden layers and discretized detection plane as output. Our P-DNN can be divided into two parts: the first layer is a common layer for preprocessing input information, and the second layer is an alternative task-specific classification layer. We divide the detection output plane that corresponds to handwritten digits into six discrete regions, representing digits 0-5. When illuminating plane wave to the object (a mask of a specific shape), the amplitude-encoded incident information of equal phase was obtained. The diffractive light was focused on the corresponding horizontally arranged detection area through a two-layer P-DNN. Then, the fashion classification was implemented by replacing the second plugin layer. The detection plane was divided into six vertically arranged discrete regions representing six fashions (T-shirts, trousers, coats, sneakers, bags, and ankle boots). Our chosen training dataset is a subset of two classic



Fig. 1 | Concept of pluggable diffractive neural networks (P-DNN) for multiple tasks. P-DNN is composed of common layers (marked in red) and classification layers (marked in blue and green, respectively). The recognition of handwritten digits and fashion datasets can be achieved by switching plugins of classification layers. When parallel light is encoded as a specific input and passed through a two-layer pluggable D<sup>2</sup>NN, the light can be focused on a specified region of the detection plane to achieve classification.

machine learning datasets, that is, Modified national institute of standards and technology (MNIST)<sup>38</sup> and Fashion-MNIST<sup>39</sup>.

The P-DNN system is trained based on the optical diffraction theory. According to the Huygens-Fresnel principle<sup>40</sup>, every point of the wavefront can be regarded as a secondary spherical wave source. Each meta-atoms within the metasurface can be treated as an optical neuron, connecting to the neurons in the next layer by diffraction.

According to the Rayleigh-Sommerfeld diffraction theory<sup>41</sup>, the complex field  $U(\mathbf{r}^{l+1})$  from *l*th to (l+1) th layer can be expressed as:

$$U(\mathbf{r}^{l+1}) = t(\mathbf{r}^{l}) \iint_{S} U(\mathbf{r}^{l}) \cdot h(\mathbf{r}^{l+1} - \mathbf{r}^{l}) \,\mathrm{d}x\mathrm{d}y \,, \quad (1)$$

for the first hidden layer with l = 1,  $U(\mathbf{r}^l)$  is the transmitted light encoded by the amplitude of the input layer. The complex field is modulated by the spatially varying complex transmittance  $t(\mathbf{r}^l) = a^l e^{i\phi^l}$ , where  $a^l$  and  $\phi^l$  are the amplitude and the phase of  $t(\mathbf{r}^l)$ . The impulse response  $h(\mathbf{r}^{l+1} - \mathbf{r}^l)$  can be defined as :

$$h\left(\mathbf{r}^{l+1}-\mathbf{r}^{l}\right) = \frac{z^{l+1}-z^{l}}{R^{2}}\left(\frac{1}{2\pi R}-\frac{1}{j\lambda}\right)\exp\left(j\frac{2\pi R}{\lambda}\right) , \qquad (2)$$

where  $\lambda$  is the illumination wavelength,  $R = \sqrt{(x^{l+1} - x_i^l)^2 + (y^{l+1} - y_i^l)^2 + (z^{l+1} - z_i^l)^2}$ , and  $j = \sqrt{-1}$ .

We explored an optimization algorithm flow based on transfer learning. The training criterion is to maximize each normalized signal corresponding to the detection region, while minimizing the total signal outside the detection region. Considering the feasibility of the experiment, a phase-only modulation method was adopted and the sigmoid function was used to restrict the phase parameter in the range of  $0-2\pi$ . During optimization, we used a mean squared error (MSE) loss function to evaluate the difference between the output and truth by light intensity of different detector regions. According to the loss function, the phase parameters are randomly optimized by using stochastic gradient descent and error backpropagation algorithm. More detailed model training and derivation are described in the Methods section and Supplementary information.

More specifically, the P-DNN training process can be divided into two steps (Fig. 2). Firstly, the common layer (MS1) and classification layer (MS2) were simultaneously trained using handwritten digital images from the MNIST datasets for the task of handwritten digits recognition. The handwritten digit inputs were trained to map to six longitudinally distributed regions representing 0–5 handwritten digits. Next, the common layer network parameters were fixed, and the parameters of the fashion classification layer (MS3) were trained using images of fashions from the Fashion-MNIST datasets. The fashion inputs were trained to map to six distributed regions representing different categories of fashions (T-shirts, trousers, coats, sneakers, bags, and ankle boots).

According to the multi-task P-DNN design process, three phases can be optimized by using handwritten



**Fig. 2 | Flowchart of multi-task P-DNN design.** The information of the input object is encoded into the amplitude channel, which propagates in free space. The propagated complex field is multiplied by the phase at each layer before being passed to the next layer. The network parameters are optimized according to the mean square error (MSE) of the output field energy. The sigmoid function is used to constrain the phase of each neuron. In the first training, the parameters of the common layer and the classification layer need to be trained simultaneously. In the subsequent training of other tasks, only the parameters of the classification layer need to be optimized. MS: metasurface

digital datasets and fashion datasets, corresponding to one sharing layer and two classification layers respectively. As a proof-of-concept, the cascaded metasurfaces are designed to realize corresponding phase modulation. The metasurfaces are composed of rectangular amorphous silicon nanofin deliberately designed on a glass substrate (Fig. 3(a)). The Berry phase modulation mechanism provides a dispersionless azimuthal angle dependent full phase control for circularly polarized light when it converts to its opposite helicity<sup>42</sup>.

The rigorous coupled wave analysis (RCWA) simulation method was used to design and optimize amorphous silicon nanofins. The electromagnetic response of each periodic array of nanostructures can be calculated. The height of the nanofins is fixed at 600 nm and the period is 500 nm in the *x* and *y* directions. The incident wavelength is 800 nm. Then, we obtained the simulated magnitudes of the circularly cross- and co-circularly polarized transmission coefficients of the nanofins by sweeping the length and width of the nanofins in 5 nm steps from 70 nm to 300 nm (Fig. 3(b)). Finally, we choose a nanofin with length L of 210 nm and width Wof 135 nm (marked with white dots) to construct metasurfaces. The angle between the long axis of the nanofin and the x-axis of the substrate is  $\varphi$  as shown in Fig. 3(c). When the incident light is set as circularly polarized light, the phase modulation value obtained by rotating the nanofin is explored under cross circularly polarized

state. The relationship between the additional phase and amplitude is related to the rotation angle of the nanofin, shown in Fig. 3(d). The additional phase can cover the range from  $0-2\pi$ .

We build experimental system to demonstrate the performance of metasurface-based multi-task P-DNN (Fig. 4(a)). Considering the characteristics of the geometric phase modulation mechanism, a linear polarizer and a 1/4 wave plate were used to generate the polarization state. The beam carrying the target information was generated by digital micromirror devices (DMD). In order to avoid the diffraction of the input beam during transmission, the 4f system was used to image the encoded target images to the front of the metasurface with distance of 4 mm as set in design. The pattern of the detection plane was collected and amplified by the microscope objective and the polarization state was filtered by the second set of quarter-wave plates and a linear polarizer. Finally, the camera was used to detect the images of the output plane.

We used two 3D displacement platforms to help align the cascaded metasurfaces. The distance between the two metasurfaces is set to 500 µm. Furthermore, a large pixel consisting of a 10×10 array of nanofins was intentionally created by repeatedly placing nanofins with the same azimuth angle. The size of the metasurface is 500×500 µm<sup>2</sup> and contains 100×100 pixels. The side length of each super-pixel is 5 µm. Figure 4(b) exhibits the scanning

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**Fig. 3** | **Design of the nanostructure based on geometric phase principle.** (a) Schematic of an amorphous silicon nanorod fabricated on a glass substrate, where  $P_x$  and  $P_y$  are periods in the *x* and *y* directions, *H* is the height, and *L* and *W* are the length and width, respectively. (b) Amplitude map of the circular transmission coefficient in cross- and co-polarization for different geometry sizes. (c) Schematic diagram of the deflection angle of the nanofin. (d) Relationship between the rotation angle of the nanofin and the additional phase.



**Fig. 4 | Experimental setup and the SEM images of the metasurface. (a)** Schematic of the experimental setup for observing the object classification. P: linear polarizer, QWP: quarter waveplate, MS: metasurface, MO: microscope objective. (b) The SEM images of the metasurface in the top and side view, respectively. A large pixel consisting of a 10 × 10 array of nanofins is marked by red dotted lines.

electron microscope (SEM) images of the top and side views of the sample.

In digit classification simulation, the P-DNN handwritten digits classification component has been iteratively trained for 10 periods, and the simulation test accuracy has reached 91.8% (Fig. 5(a)). We used 6000 handwritten digit images as the test datasets, and randomly selected 300 images of datasets as the experimental validation datasets (50 images per classification category). The test results are presented using the confusion matrix, showing test details for correctly identified and misidentified instances of simulation and simulation (Fig. 5(b, c)). According to the experimental statistical results, the test accuracy reaches 90%. The experimental results are consistent well with the simulated res-

ults, indicating that the design theory is effective. The handwritten digital image was encoded into the amplitude channel as input (Fig. 5(d)). The light intensity distribution of the detection plane obtained in the simulation and experiment is shown in Fig. 5(e, f). By analyzing the energy distribution of the detection (Fig. 5(g)), The results show that the system can rightly recognize handwritten digits according to the energy distribution. Due to the influence of experimental error, the maximum energy distribution of experimental results is a bit lower than simulation results. In order to clearly display the difference between the percentage of maximum and second maximum energy, we have introduced  $\Delta E = E_{\text{max}}$  (maximum energy)  $- E_{\text{smax}}$  (second maximum energy) as an indicator of the energy distribution difference,



Fig. 5 | Simulation and experiment result of num-P-DNN. (a) Training accuracy is 92% after training 10 epochs. (b, c) Simulation and experimental results of confusion matrix for handwritten digits. The Simulation and experimental results test accuracy is 91.8% and 91.3% respectively, which is obtained by dividing the sum of elements on the main diagonal of confusion matrix by the sum of all elements. (d) Handwritten digital input images were encoded into amplitude channel. (e, f) Output energy distribution maps of handwritten digits in simulations and experimental results.  $\Delta E$  represents the difference between the percentage of maximum and second maximum energy.

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where blue numbers represent simulation data and red numbers represent experimental data. It can be observed that the maximum energy is at least 71% higher than the second maximum energy in simulations, and at least 34% higher in experiments. The results indicate that P-DNN is capable of achieving high recognition accuracy and is not easily affected by errors.

Furthermore, we test the classification performance of P-DNN on more complex image datasets, by replacing the classification layer plug-in for fashion recognition. The datasets consist of six different fashion products (Tshirts, pants, jumpers, sneakers, bags, and ankle boots). It is worth noting that the training of the fashion plugin has achieved high classification accuracy after only five training epochs. Compared to the training without transfer learning, the training time and parameters are reduced by half. We used 6000 fashion images as the test dataset, the numerical test has an accuracy rate of 90.2% (Fig. 6(a)). As above, we used the confusion matrix to display the statistical results, and selected 300 images from the test datasets for experimental verification (Fig. 6(b, c)). It can be seen that the experimental test accuracy reached 90%. Figure 6(d) shows the fashion images which were encoded to the amplitude channel. The system successfully realizes the classification of fashion according to the energy distribution of the output plane (Fig. 6(e, f)). It turned out that P-DNN only needs a small amount of retraining based on the original para-



Fig. 6 | Simulation and experiment result of fashion-P-DNN. (a) Training accuracy is 91% after training 5 epochs. (b, c) Simulation and experimental results of confusion matrix for fashions classification. The Simulation and experimental results test accuracy is 90.2% and 90% respectively, which is obtained by dividing the sum of elements on the main diagonal of confusion matrix by the sum of all elements. In the simulation and experimental results, the test accuracy reaches 90.2% and 90%, respectively. (d) Fashion input images were encoded into amplitude channel. (e, f) Output plane energy distribution maps of fashions in simulations and experiments. (g) Energy distribution percentage of experimental and simulated results of fashions.  $\Delta E$  represents the difference between the percentage of maximum and second maximum energy.

meters, and other more difficult tasks can also achieve good recognition performance.

# Conclusions

Generally, the D<sup>2</sup>NN can only achieve a single task after the design is completed and the physically manufactured network cannot be modified. If other tasks need to be achieved, D<sup>2</sup>NN needs to be completely retrained and manufactured. Here we demonstrate that P-DNN can be applied to recognize various tasks in the near-infrared band by switching internal plug-ins. To verify the feasibility, we design cascaded metasurfaces for handwritten digits and fashion recognition. It can work similarly to the pluggable components in optical communication. According to user requirements, classification layer (pluggable layer) plug-ins can be customized to be used in combination with common layer plug-ins to achieve a variety of specific tasks (not limited to classification tasks). The experimental test accuracies were 91.3% and 90.0%, respectively, which were in good agreement with the numerical simulation results. Such plug-ins have good reconfigurability and can easily complete more tasks through plugging and unplugging. It has the characteristics of ultra-low energy consumption and lightspeed calculation, and may provide extra flexibility for neural networks. Our proposed P-DNN can achieve a wide range of applications, such as intelligent optical filtering in microscopy imaging and real-time object detection in autonomous driving systems.

# Material and method

# Training of the P-DNN

Our P-DNN is trained using Python version 3.7.0. and TensorFlow framework version 2.4.1 (Google Inc.) on a desktop computer (Intel(R) Core(TM) i5-10500 CPU @3.10 GHz with 32 GB RAM, running the Windows 10 operating system (Microsoft)). In the training process, mean square error loss is selected as the loss function, which is usually used for target classification of machine learning, and the Adam optimizer is used to update the phase value of each layer in the network. We used 36000 handwritten digital images and fashion images as training datasets with a training batch size of 8 and a learning rate of 0.01.

# Fabrication

The dielectric metasurface of amorphous silicon ( $\alpha$ -Si) nanofins was fabricated on SiO<sub>2</sub> substrate. Firstly,

amorphous silicon films with a thickness of 600 nm were prepared by plasma-enhanced chemical vapor deposition. Subsequently, the polymethyl methacrylate resist layer was spin-coated. The pattern is then patterned using standard electron beam lithography. After development, a 30 nm thick chromium layer is plated on the surface of the sample. Finally, we performed the lift-off process in hot acetone and employed inductively coupled plasma reactive ion etching to transfer the desired structure from chromium to silicon.

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#### Author contributions

L. L. Huang proposed the idea, C. He, H. Q. Zhou, and X. Li developed the optimization algorithm, C. He and L. L. Huang conducted the designs and numerical simulations, Y. Li and J. J. Li fabricated the samples, C. He, D. Zhao and F. Fei performed experiment the measurements, C. He, L. L. Huang, F. Dong and Y-X. Miao analyzed the data, C. He, L. L. Huang, and H. Q. Zhou prepared the manuscript. L. L. Huang and Y. T. Wang supervised the overall projects. All the authors analyzed and discussed the results.

#### Competing interests

The authors declare no competing financial interests.

## Supplementary information

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