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Nanobridged rhombic antennas supporting both dipolar and high-order plasmonic modes with spatially superimposed hotspots in the mid-infrared

En-Ming You^{1,†}, Yiqin Chen^{2,†}, Jun Yi^{1,†}, Zhao-Dong Meng¹, Qian Chen¹, Song-Yuan Ding^{1*}, Huigao Duan^{2*}, Martin Moskovits³ and Zhong-Qun Tian¹

Mid-infrared antennas (MIRAs) support highly-efficient optical resonance in the infrared, enabling multiple applications, such as surface-enhanced infrared absorption (SEIRA) spectroscopy and ultrasensitive mid-infrared detection. However, most MIRAs such as dipolar-antenna structures support only narrow-band dipolar-mode resonances while high-order modes are usually too weak to be observed, severely limiting other useful applications that broadband resonances make possible. In this study, we report a multiscale nanobridged rhombic antenna (NBRA) that supports two dominant resonances in the MIR, including a charge-transfer plasmon (CTP) band and a bridged dipolar plasmon (BDP) band which looks like a quadruple resonance. These assignments are evidenced by scattering-type scanning near-field optical microscopy (s-SNOM) imaging and electromagnetic simulations. The high-order mode only occurs with nanometer-sized bridge (nanobridge) linked to the one end of the rhombic arm which mainly acts as the inductance and the resistance by the circuit analysis. Moreover, the main hotspots associated with the two resonant bands are spatially superimposed, enabling boosting up the local field for both bands by multiscale coupling. With large field enhancements, multiband detection with high sensitivity to a monolayer of molecules is achieved when using SEIRA. Our work provides a new strategy possible to activate high-order modes for designing multiband MIRAs with both nanobridges and nanogaps for such MIR applications as multiband SEIRAs, IR detectors, and beam-shaping of quantum cascade lasers in the future.

Keywords: optical antenna; charge transfer plasmon; multiband resonances; scanning near-field optical microscopy; surface-enhanced infrared spectroscopy

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¹State Key Laboratory of Physical Chemistry of Solid Surfaces, Collaborative Innovation Center of Chemistry for Energy Materials, College of Chemistry and Chemical Engineering, Xiamen University, Xiamen 361005, China; ²National Engineering Research Center for High Efficiency Grinding, College of Mechanical and Vehicle Engineering, Hunan University, Changsha 410082, China; ³Department of Chemistry and Biochemistry, University of California, Santa Barbara, California, 93106, USA.

'Correspondence: SY Ding, E-mail: syding@xmu.edu.cn; HG Duan, E-mail: duanhg@hnu.edu.cn Received: 17 June 2021; Accepted: 3 September 2021; Published online: 30 December 2021

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[†]These authors contributed equally to this work.

Introduction

Mid-infrared antennas (MIRAs), often constructed from metals (e.g., Au, Al or Ag), highly doped III-V semiconductors, electron-doped graphene or phonon-polaritonbased nanostructures1-11, support optical resonance in the mid-infrared spectral range (400 to 4000 cm⁻¹). MIR-As can act as receiving antennas thereby concentrating mid-infrared beams from free space to nanoscale regions (termed as hotspots) in the vicinity of the surface of MIRAs¹². MIRAs can also act as transmitting antennas to directionally amplifying thermal radiation produced by local heating of sources coupled to MIRAs¹³. These impressive features of MIRAs have inspired a wide range of investigation of their potential applications for surface-enhanced infrared absorption (SEIRA) spectroscopy leading to ultrahigh sensitivities (up to hundreds of oscillators)14, for biological and chemical sensors in the mid-infrared region^{15–18}, for beam-shape engineering of quantum cascade lasers (QCL)19, and for highly-responsive photodetectors²⁰ with enhanced absorption and photocarrier collection efficiency in the mid-infrared²¹. The core elements for the high-performance applications are the MIRA micro- and nanostructures, but the development of MIRA structures lags far behind that of optical antenna nanostructures in the visible spectral range²².

Single-arm dipolar-antenna structures are among the most classical MIRAs, often consisting of gold rods with tunable resonant wavelengths by tuning the length of the rods²³⁻²⁶. Furthermore, dual-arm dipolar-antennas with nanometer-sized gaps (nanogaps), such as gold rod dimers, have also been developed on account of the strength of the local field enhancement factors (LFEFs, $|E_{loc}/E_0|^2$) in their nanogaps^{27,28–29}. Nevertheless, both single-arm and dual-arm dipolar-antennas usually support only the dipolar resonance mode which is a fundamental and narrow-band mode with a typical bandwidth around 200 -500 cm⁻¹. Usually, high-order modes in single-arm or dual-arm are typically too weak in the optical spectra^{26,28,30}. This feature limits the application demanding multiple resonances in MIR region, such as SEIRA with a broad range so as to measure molecular vibrational absorption bands in fingerprint range 500 -1500 cm⁻¹ and functional group range 1500 -4000 cm^{-1 31}.

To obtain multiband MIRAs, several micro- and nanostructures beyond single-arm or dual-arm antennas have been designed, among them, gold nano-crosses^{32,33}, nanoaperture structures^{34,35}, fractal microstructures^{36–38},

log-periodic trapezoidal structures³⁹, and dipolar antennas with multiple lengths^{40–42}. These structures could be categorized into the micro- and nanostructures supporting several dipolar modes. Fundamentally, it is a long-term challenge to develop single-arm or dual-arm antennas supporting simultaneously pronounced fundamental and high-order plasmonic modes such as a quadrupolar mode.

In this study, we develop a nanobridged rhombic antenna (NBRA) exhibiting two pronounced resonancebands in the MIR regions. The two bands are assigned to a charge-transfer plasmon (CTP) mode and a bridged dipolar plasmon (BDP) mode, which are demonstrated by the scattering-type scanning near-field optical microscopy (s-SNOM), a technique that is widely used to image the near-field distribution of plasmonic modes^{43–47}. The nanobridge structure and the linked rhombic-arm antennas effectively controls the resonant frequencies and extinction intensities of the CTP and BDP bands. The s-SNOM also demonstrates that the main hotspots of the two bands are spatially overlapped. This feature enables us to boost up the local field enhancement of both bands via NBRA dimers with nanogaps. Moreover, one order of magnitude of additional enhancement can be obtained for both bands from a hybrid structure consisting of an NBRA dimer, a sandwiched dielectric spacer layer and a gold reflector. Such high field enhancement enables detecting a monolayer of molecules using the two absorptions located in the two bands.

Materials and methods

Numerical simulations

All electromagnetic simulations were performed by the commercial software COMSOL Multiphysics based on the finite element method. The simulation space was a cuboid, whose sizes along the long and short axes of the NBRA were equal to the fabricated arrays. The perfectly matched layers were used for the top and bottom boundaries while the periodic conditions were employed for the side boundaries. The polarization of the incident electric field was either parallel or perpendicular to the long axis of the antenna and the resulting transmittance or reflectance spectra were averaged to approximate the unpolarized illumination used in the experiment. Corners and edges of the gold nanostructure were rounded by a radius of 10 nm for a reasonable simulated local-field distribution there. The mesh size was set as 0.5 nm for each dimension of the nanostructure and its close proximity and gradually became coarser toward the outer

borders of the simulation domain. The mesh sizes of different parts are listed in Table S1. The convergence condition is satisfied (Fig. S2, Supplementary information). All the $|E_z|$ and φ_z were evaluated in the plane 50 nm above the top surface of the NBRA structure. The LFEF was evaluated at the point 2 nm away from the extremity of the structure and 15 nm above the CaF₂ substrate. The refractive index for CaF₂ was 1.41, and the dielectric constants for gold were adapted from literature⁴⁸.

Fabrication of NBRAs

All the NBRAs were fabricated on the CaF2 substrate or on the reflective substrate by sequentially using electronbeam lithography, metal deposition and "Sketch and Peel" lithography (SPL)⁴⁹⁻⁵³. First, a hydrogen silsequioxane (HSQ) resist (XR-1541-006, Dow Corning) was spin-coated on the substrate at the speed of 4000 rpm. Then, a conductive polymer (ESPACER, Showa Denko) layer of 30 nm was casted on the HSQ resist to avoid pattern distortions due to the charging effect. The sample was then directly loaded into electron-beam direct writing system (Raith 150 Two). The exposure was executed by an electron beam with an accelerating voltage of 30 kV and a beam current of 280 pA. Before the development, the top layer of conductive polymer should be removed by DI water for 10 s, and then a salty developer (1%wt NaOH + 4%wt NaCl aqueous solution) was used to chemically etch the unexposed HSQ resist for 1 min. To stop further development, the structured substrate was immediately rinsed by DI water. The dipping in isopropanol reduced the surface tension and further helped us to obtain the upright HSQ thin-wall structures on the substrate after blow-drying of nitrogen gas steam.

Metal deposition was applied by a thermal evaporation system. The working chamber was pre-pumped to the pressure of 1×10^{-5} Pa, and the working pressure was kept at the value of 5×10^{-5} Pa. Due to the requirement of peeling off gold film, the deposition of adhesive metal was excluded from our fabrication process. A 30-nm thick gold film was obtained at a rate of 5 angstrom/s. The thickness was monitored by a quartz-crystal microbalance possessing the sensitivity of angstrom.

The standard process of SPL was reported in our previous literature $^{49-53}$. To figure out the influence of HSQ in optical measurement, a vapor-HF chemical etching was used to remove HSQ templates. To avoid the condensation of $\rm H_2O$ byproduct in etching, the sample was kept at the temperature of $\rm 40^{\circ}C$.

Scanning electron microscopy

The morphology of resultant substrates was characterized by a field-emission scanning electron microscope (SIMG-HD, Carl-ZEISS). To avoid the charging effect during the imaging process, the accelerating voltage and the working distance were set as 1 kV and 3 mm, respectively.

FTIR microscopy measurements

A commercial FTIR spectrometer (Thermo Fisher Nicolet iN10) was used to perform all transmittance and reflectance measurements. The instrument is equipped with a silicon carbide (globar) light source, a KBr beam splitter, Cassegrain objective (15×, N.A. = 0.4, incident angle θ ranging between 10 and 44°) and a mercury cadmium-telluride (MCT) detector. The transmittance or reflectance of the antennas were defined as the signal intensities transmitted/reflected from the antenna divided by those from a background taken at a blank area on the substrate. Each spectrum was acquired by averaging 64 spectra with a 3 cm⁻¹ spectral resolution. A 100 × 100 μm² square collection aperture was used for all the measurements. The SEIRA spectra were obtained by subtracting the baseline (generated by asymmetric least-squares smoothing algorithm)⁵⁴ from the original data. The incident and collected light are unpolarized light.

Scattering-type scanning near-field optical microscopy (s-SNOM) measurement

The s-SNOM system (neaspec GmbH) was employed to perform the near-field amplitude and phase imaging of the NBRA structures. A silicon atomic force microscopy (AFM) tip (Nanosensors, PPP-NCH) worked as the scatterer to transform the near-field signals to the far field, when the tip and the antenna sample were illuminated by the focused beam of a continuously tunable QCL source. The illuminating beam was incident at ~50° referring to the surface normal, and its polarization was parallel to the long axis of the NBRA structure (s-polarized light). The signals backscattered by the tip were detected with a pseudo-heterodyne interferometer⁵⁵. The vertical (p-polarized) components of the signals were selected by using a polarizer in front of the detector. To obtain a modulation of the distance between tip and antenna, the tip was oscillating vertically at a frequency Ω≈250 kHz with an amplitude of ~100 nm. Demodulation of the detected signals at the third harmonic frequency (3Ω) yielded almost background-free amplitude and phase signals $|s_3|$ and φ_3 .

Functionalization with PNTP molecules of the antennas

The sample was incubated in an ethanolic solution of 4-nitrothiophenol (PNTP, 98%, Matrix Scientific) for 12 hours and then was rinsed with a large amount of ethanol (AR, Sinopharm Chemical Reagent Co., Ltd) to remove physically adsorbed molecules, and finally was dried with nitrogen. The concentration of the ethanolic solution of PNTP was kept constant at 1 mM.

Results and discussion

NBRA structure and optical properties

The NBRA (Fig. 1(a, c) and Fig. S3(a), Supplementary in-

formation) consists of two rhombic arms connected with each other by a nanobridge (about 30 nm in width and 130 nm in length). Each arm contains a sharp tip (the corner angle α in Fig. 1(d) is 30°) with a radius of curvature about 10 nm. The thickness (t_0) and total length (l_0) of NBRA are 30 nm and 2800 nm, respectively. The NBRA arrays were fabricated by the SPL method which is appropriate for fabricating multiscale metallic patterns with high-fidelity features and nanogaps (see Materials and methods for details)^{49–53}. The periodicities along the long and short axis of the NBRA are 3600 nm and 1000 nm. The experimental and simulated transmittance spectrum (Fig. S4, Supplementary information), as

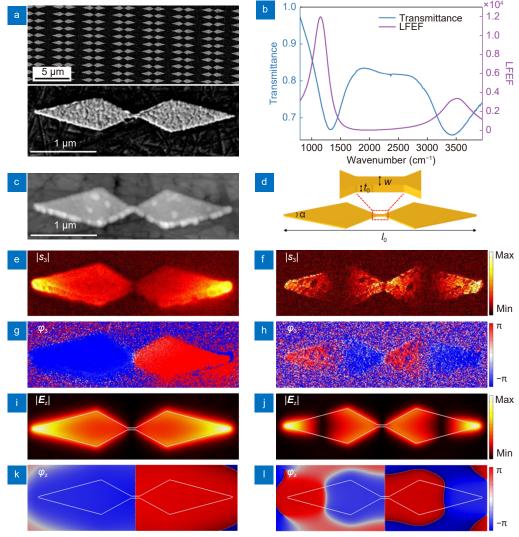


Fig. 1 | (a) Scanning electron microscopy (SEM) image of NBRA structures. (b) Experimental transmittance of the NBRA array (blue curve) and simulated LFEF at the extremities of the structure (purple curve). (c) AFM topography of a single NBRA structure. The scale bars are 1 μ m. (d) Sketch and parameters of the NBRA structure, consisting of two rhombic arms connected with each other by a nanobridge. The thickness (t_0) and total length (l_0) of NBRA are 30 nm and 2800 nm. The nanobridge is 30 nm in width and 130 nm in length. The radius of sharp tip of each arm is 10 nm and α is 30°. (e-h) Measured near-field (e, f) amplitude and (g, h) phase of single NBRA structure at 1100 cm⁻¹ and 2100 cm⁻¹, respectively. (i–l) Simulated | E_z | (i, j) and φ_z (k, l) of single NBRA structure at 1100 cm⁻¹ and 2100 cm⁻¹, respectively.

well as the simulated LFEF (Fig. 1(b)), show that the NBRA supports two pronounced resonance bands. One band is centered at 1319 cm⁻¹, the other is centered at 3425 cm⁻¹. The simulated transmittance spectra also show that the resonant absorption of the NBRA structure in the mid-infrared range only occurs when the polarization is along the long axis of the NBRA (Fig. S5, Supplementary information). To assign the plasmonic modes associated with the two bands, we employed the s-SNOM with the pseudo-heterodyne interferometric detection module which can provide almost background-free near-field amplitude and phase (see Methods for details)46,47,55, to carry out the near-field imaging of the NBRA. Due to the limited output range of the QCL source in our laboratory, we choose 1100 cm⁻¹ and 2100 cm⁻¹ for the imaging of each band.

The measured near-field amplitude image exhibits two hotspots at the two extremities of the structure (Fig. 1(e)) when illuminating with a continuum-wave beam at 1100 cm⁻¹ from the QCL, which is in accord with the simulated $|E_z|$ (Fig. 1(i)). Parallelly, the measured near-field phase image exhibits a phase jump of $\sim \pi$ at the center of the nanobridge (Fig. 1(g)), in accord with the simulated phase image φ_z (Fig. 1(k)), and provides direct experimental evidence for the anti-phase field oscillating at 1100 cm⁻¹. This mode was assigned to the charge-transfer plasmon (CTP) mode⁵⁶⁻⁵⁸, in which the current density is mainly confined at the nanobridge (Fig. S6(a), Supplementary information). The CTP mode is different from the dipolar mode of a single-arm antenna in which the current density is distributed along the antenna except for the two ends (Fig. S6(c), Supplementary information).

To assign the plasmonic mode associated with the band centered at 3425 cm⁻¹, we performed the s-SNOM imaging at 2100 cm⁻¹ (4.76 µm) which corresponds to the shortest wavelength of the QCL source in our laboratory. The simulated LFEF at 2100 cm⁻¹ is around 25, which means the s-SNOM signals would be rather weak. In spite of this, the simulated charge distribution (Fig. S7, Supplementary information) shows similar characteristic between 2100 cm⁻¹ and 3425 cm⁻¹. Thus the s-SNOM imaging still allows us to distinguish the plasmonic mode of this band. The measured near-field amplitude (Fig. 1(f)) and the simulated $|E_z|$ (Fig. 1(j)) show relatively strong signals at the two extremities of each rhombic arm as well. Notably, the measured near-field phase (Fig. 1(h)) and simulated φ_z (Fig. 1(l)) show phase

jumps of $\sim \pi$ at three locations: the center of each rhombic arm and the center of the nanobridge. This mode looks like two dipoles coupled through the nanobridge, and thus was named as the bridged dipolar plasmon (BDP) mode in which the current density is mainly confined at the nanobridge (Fig. S6(b), Supplementary information). Moreover, the main hotspots of both bands (Fig. 1(e), 1(f) and Fig. S8, Supplementary information) are spatially superimposed at the extremities of NBRA structure, where the LFEFs are $\sim 1.3 \times 10^4$ for the CTP and $\sim 3.4 \times 10^3$ for the BDP according to the electromagnetic simulations (Fig. 1(b)).

The NBRA excites the high-order mode more efficiently than the nanobar. The extinction spectra of the NBRA and the nanobar monomer both show two resonant bands in the mid-infrared range (Fig. S9(a), Supplementary information). The extinction intensities of the NBRA at the first and second band are 8.3% and 156.1% larger than those of the nanobar (Fig. S9(a), Supplementary information). Meanwhile, the resonant wavenumbers of the NBRA are slightly red-shift compared with that of the nanobar. And the full width at half maximum (FWHM) of the resonant bands of the NBRA are broader than those of the nanobar (Table S2, Supplementary information).

Comparing with other nanobridged structures, such as nanobridged-disks (Fig. 2(b)) or rectangles (Fig. 2(c)), the NBRA (Fig. 2(a)) shows distinct multiband resonances in the mid-infrared region in the simulated extinction spectra (Fig. 2(d)). Further, the hotspots of the NBRA are located at the extremities of the structure (Fig. 2(f)), while the hotspots of nanobridged-disks or rectangles at the CTP resonance are distributed dispersively (Fig. 2(g) and 2(h)), resulting to ten times lower LFEFs than that of the NBRA (Fig. 2(e)).

The CTP and BDP bands of the NBRA are strongly associated with the geometrical parameters of the nanobridge. Figure 3(a) shows that the CTP band redshifts and weakens, and the BDP band redshifts and broadens as the width of the nanobridge decreases from 30 nm to 5 nm. As the nanobridge is broken and transforms to a nanogap in between the two arms, the BDP band disappears in their stead a bonding dipolar plasmonic mode (Fig. 3(b)) and a bonding quadrupolar plasmonic mode (Fig. 3(c)) appears. In contrast, as the width of the nanobridge increases from 30 nm to 370 nm, the CTP band blueshifts and strengthens, and the BDP band blueshifts and weakens. Ultimately, the CTP and BDP bands evolve

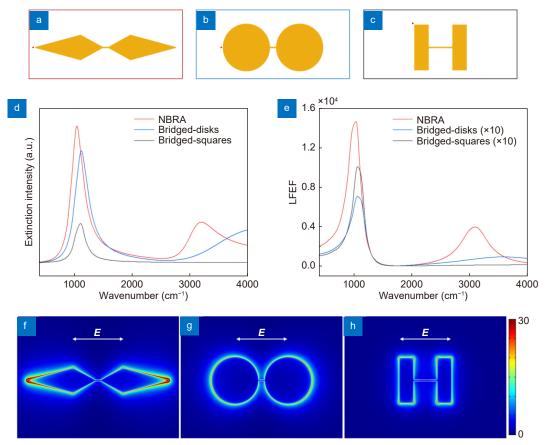


Fig. 2 | The model of (**a**) NBRA, (**b**) nano-bridged disks and (**c**) nano-bridged rectangles. All the structures are placed on the CaF₂ substrate. The incident polarizations are along the long-axis of the nanobridge. The thickness and the width of the nanobridge are 30 nm for all three structures. The lengths of the nanobridges are 130 nm for the NBRA and the nanobridged-disks, and 500 nm for the nanobridged-rectangles. The total length of the NBRA is 3000 nm. The radius of the disks are 500 nm. The length and width of the rectangles are 962 nm and 308 nm, respectively. The red points in (a–c) are the positions where the LFEFs are evaluated. The LFEF was evaluated at the point 2 nm away from the structure along the long axis and 15 nm above the CaF₂ substrate for the NBRA and the nanobridged-disks. While for the nanobridged-rectangles, the evaluating point is 2 nm away from the corner of the rectangle. (**d**) The simulated extinction spectra and (**e**) the LFEFs of all three structures. Effeld distributions at the CTP resonance for (**f**) the NBRA, (**g**) the nanobridged-disks and (**h**) the nanobridged-rectangles.

to a typically dipolar band (Fig. 3(d)) and quadrupolar band (Fig. 3(e)), respectively, similar to that in a nanobar antenna of the same length (Fig. S10, Supplementary information).

An circuit model consisting of resistances (R), inductances (L) and capacitors (C) was built to understand the role of the nanobridge width-tuned plasmonic resonant frequencies and extinction intensities. As shown in the inset of Fig. 4(a), each rhombic arm as well as the nanobridge was modelled as a parallel RLC circuit, and all of three circuits were further connected in series. The total impedance of the circuits system is:

$$Z\left(\omega\right) = \frac{\omega L_{\rm b} R_{\rm b}}{\omega L_{\rm b} + {\rm i} R_{\rm b} (1 - \omega^2 L_{\rm b} C_{\rm b})} + \frac{2\omega L_{\rm 0} R_{\rm 0}}{\omega L_{\rm 0} + {\rm i} R_{\rm 0} (1 - \omega^2 L_{\rm 0} C_{\rm 0})} \ . \tag{1}$$

The extinction spectrum is proportional to the real part of Z^{59} .

$$\begin{split} Re\left(Z\left(\omega\right)\right) = & \frac{\omega^{2}L_{b}^{2}R_{b}}{R_{b}^{2}L_{b}^{2}C_{b}^{2}\omega^{4} + \omega^{2}\left(L_{b}^{2} - 2R_{b}^{2}L_{b}C_{b}\right) + R_{b}^{2}} \\ + & \frac{2\omega^{2}L_{0}^{2}R_{0}}{R_{0}^{2}L_{0}^{2}C_{0}^{2}\omega^{4} + \omega^{2}\left(L_{0}^{2} - 2R_{0}^{2}L_{0}C_{0}\right) + R_{0}^{2}} \;, \end{split} \tag{2}$$

where R_b , L_b and C_b are the resistance, inductance and capacitance of the nanobridge and all depend on the width of the nanobridge; R_0 , L_0 and C_0 are the resistance, inductance and capacitance of each rhombic arm and are also all dependent on the nanobridge width since the geometric cross section of one end of each rhombic arm and that of the linked nanobridge are the same.

Herein, $L_{\rm b}$ is the sum of conventional magnetic inductance $L_{\rm M} \sim \frac{\mu_0 l_0}{2\pi} \ln \frac{l_0}{w+h}$ 57,59,60, and the kinetic inductance $L_{\rm K} = \frac{l_0}{wh\epsilon_0 \omega_p^2}$ 61,62, where ϵ_0 and μ_0 are, respectively, the permittivity and the permeability of free space, l_0 , w and h are, respectively, the length, width, and height of

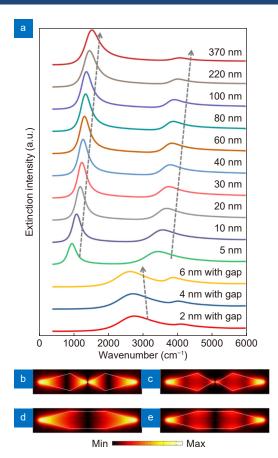


Fig. 3 | (a) Simulated extinction spectra of NBRA structure with different nanobridge width. (b–c) Simulated mapping of $|E_z|$ of bonding dipolar plasmonic band (b) and bonding quadrupolar plasmonic band (c) of a single NBRA structure with a broken nanobridge and 4 nm gap size. (d–e) Simulated mapping of $|E_z|$ at CTP band (d) and BDP band (e) with 370 nm nanobridge width.

the nanobridge; and ω_p is the plasma frequency of the metal. Thus, $L_{\rm b}$ can be written as $L_{\rm b} \sim \left(\frac{a_1}{w} + a_2 \ln \frac{a_3}{w}\right)$, where a_1 , a_2 and a_3 are fitting parameters. The inductance of the rhombic arms obeys the same expression as $L_0 \sim \left(\frac{b_1}{w} + b_2 \ln \frac{b_3}{w}\right)$. $C_{\rm b}$ and C_0 linearly depend on the nanobridge width^{59,60}, $C_{\rm b} \sim (c_1 w + c_2)$ and $C_0 \sim (d_1 w + d_2)$.

In this study, we considered the essential impact of R_b and R_0 on the extinction intensities of both bands, which have not been considered in the previous study⁵⁶. Taking the featured geometries of the NBRA structure, we derived the w-dependent R_b and R_0 :

$$R_{\rm b} \sim \left(\frac{e_1}{e_2 - w} \ln \frac{e_2}{w} + \frac{e_3}{w}\right) , \qquad (3)$$

$$R_0 \sim \left(\frac{f_1}{f_2 - w} \ln \frac{f_2}{w} + \frac{f_3}{w} + f_4\right) .$$
 (4)

The detailed derivations of R_b and R_0 as a function of

nanobridge width are described in Supporting Information section 1. The aforementioned $b_{1,2,3}$, $c_{1,2}$, $d_{1,2}$ $e_{1,2,3}$, and $f_{1,2,3,4}$ are all fitting parameters.

Fitting $Re(Z(\omega))$ containing all 17 fitting parameters in a one-step fit is too complicated to be realized. Instead, we used a two-step fit to obtain all the fitting parameters, as shown in Table 1. The detailed fitting procedures are described in Supporting Information section 2. Consequently, we got the w-dependent L_b , L_0 , C_b , C_0 , R_b and R₀ curves (Fig. S11, Supplementary information) and $Re(Z(\omega))$ spectra (Fig. S12, Supplementary information). Fig. 4(a) and 4(b) shows that the w-dependent resonant frequencies and intensities which were extracted from the two dominant bands in the w-dependent spectra of $Re(Z(\omega))$ (Fig. S12, Supplementary information) match well with the w-dependent resonant frequencies and extinction intensities of the CTP and BDP bands which were extracted from the simulated extinction spectra (Fig. 3(a)).

The analytical form of $Z(\omega)$ enables us to explore the main factors affecting the resonant frequencies. Typically, the resonant frequencies of an RLC circuit make the imaginary part of $Z(\omega)$, as shown in Eq. (5), be zero.

$$\begin{split} \operatorname{Im}\left(Z\left(\omega\right)\right) = & \frac{\omega R_{\mathrm{b}}^{2} L_{\mathrm{b}} (L_{\mathrm{b}} C_{\mathrm{b}} \omega^{2} - 1)}{R_{\mathrm{b}}^{2} L_{\mathrm{b}}^{2} C_{\mathrm{b}}^{2} \omega^{4} + \omega^{2} \left(L_{\mathrm{b}}^{2} - 2 R_{\mathrm{b}}^{2} L_{\mathrm{b}} C_{\mathrm{b}}\right) + R_{\mathrm{b}}^{2}} \\ + & \frac{2\omega R_{\mathrm{o}}^{2} L_{\mathrm{o}} (L_{\mathrm{o}} C_{\mathrm{o}} \omega^{2} - 1)}{R_{\mathrm{o}}^{2} L_{\mathrm{o}}^{2} C_{\mathrm{o}}^{2} \omega^{4} + \omega^{2} \left(L_{\mathrm{o}}^{2} - 2 R_{\mathrm{o}}^{2} L_{\mathrm{o}} C_{\mathrm{o}}\right) + R_{\mathrm{o}}^{2}} \; . \end{split}$$
(5)

However, the exact solutions to Eq. (5) are too complicated to be further analyzed. Instead, we adopted commonly used simplification, independently making the first term or the second term of Eq. (5) be zero. Then we got the simplified solutions:

$$\omega_1 = \frac{1}{\sqrt{L_b C_b}} \ . \tag{6}$$

$$\omega_2 = \frac{1}{\sqrt{L_0 C_0}} \ . \tag{7}$$

It can be found that, ω_1 and ω_2 correspond to the RLC resonances of the independent nanobridge and rhombic arm respectively. Furthermore, Eqs. (6, 7) are good approximations for ω_{CTP} and ω_{BDP} , because the deviations between $\omega_{1,2}$ and $\omega_{\text{CTP},\text{BDP}}$ extracted from the $Re\left(Z(\omega)\right)$ spectra are less than 1%, as shown in Fig. S13 (see Supplementary information).

$$\omega_{\rm CTP} pprox rac{1}{\sqrt{L_{
m b}C_{
m b}}} \; ,$$
 (8)

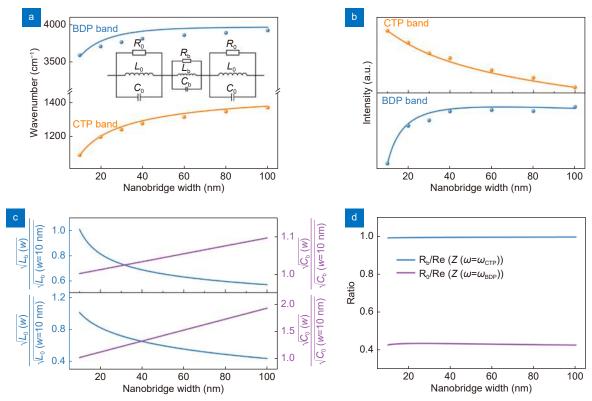


Fig. 4 | Nanobridge width-dependent (a) resonant frequencies and (b) intensities of CTP and BDP bands. The orange and blue circles are extracted from the simulated extinction spectra (Fig. 3(a)), while the points on the fitting curves are extracted from the spectra of Re $(Z(\omega))$ (Fig. S12, Supplementary information). Inset in (a): RLC circuit model of the NBRA structure. (c) Nanobridge width-dependent ratio of $\frac{\sqrt{L_b(w)}}{\sqrt{L_b(w=10~\text{nm})}}$ (blue curve in the top panel), $\frac{\sqrt{C_b(w)}}{\sqrt{C_b(w=10~\text{nm})}}$ (purple curve in the top panel), $\frac{\sqrt{L_0(w)}}{\sqrt{L_0(w=10~\text{nm})}}$ (blue curve in the bottom panel) and $\frac{\sqrt{C_0(w)}}{\sqrt{C_0(w=10~\text{nm})}}$ (purple curve in the bottom panel). (d) Nanobridge width-dependent ratio of $\frac{R_b}{\text{Re}(Z(\omega=\omega_{\text{CTP}}))}$ (blue curve) and $\frac{R_0}{\text{Re}(Z(\omega=\omega_{\text{BDP}}))}$ (purple curve). R_b and R_0 are the deterministic parameters for Re $(Z(\omega))$.

Table 1 | Fitting parameters used in the RCL circuit model

Table 1 1 King parameters assault the Not circuit model			
Parameter	Value	Parameter	Value
a ₁	2.17×10 ⁻¹⁰	<i>d</i> ₁	3.82×10 ⁻¹⁹
a ₂	6.75×10 ⁻¹²	d_2	3.39×10 ⁻¹⁷
a ₃	5.74×10⁴	e ₁	9.77×10 ¹¹
<i>b</i> ₁	1.64×10 ⁻¹²	e ₂	9.03×10 ⁹
<i>b</i> ₂	5.14×10 ⁻¹³	e ₃	-7184.74
<i>b</i> ₃	650.03	f_1	3.21×10⁵
<i>c</i> ₁	1.24×10 ⁻²⁰	<i>f</i> ₂	1146.59
c_2	1.18×10 ⁻¹⁷	f ₃	-2232.04
		f_4	1

$$\omega_{\rm BDP} pprox rac{1}{\sqrt{L_0 C_0}} \ .$$
 (9)

The inductances $L_{\rm b}$ and $L_{\rm 0}$ are the determining quantities for $\omega_{\rm CTP}$ and $\omega_{\rm BDP}$ as a function of w. $L_{\rm b}$ and $L_{\rm 0}$ decrease (Fig. S11(a, b), Supplementary information), while the $\frac{1}{\sqrt{L_{\rm b}}}$ and $\frac{1}{\sqrt{L_{\rm 0}}}$ increase (Fig. 4(c)) as the nanobridge becomes wider, which is consistent with the blue shift of

 ω_{CTP} and ω_{BDP} (Fig. 4(a)). Contrarily, the $\frac{1}{\sqrt{C_b}}$ and $\frac{1}{\sqrt{C_0}}$ decrease as w increases (Fig. 4(c)). Furthermore, $\frac{1}{\sqrt{L_b}}$ and $\frac{1}{\sqrt{L_0}}$ increase more than 10% and 90% respectively while $\frac{1}{\sqrt{C_b}}$ and $\frac{1}{\sqrt{C_0}}$ both decrease around 50% as w increases from 10 nm to 100 nm.

To study the key quantities to determine the extinction intensities (Fig. 4(b)) of both bands ($\sim \text{Re}(Z(\omega = \omega_{\text{CTP}}, \omega_{\text{BDP}}))$), we substituted Eqs. (8) and (9) into Eq. (2), and got,

$$\operatorname{Re}\left(Z(\omega=\omega_{\mathrm{CTP}})\right) = \frac{2L_{0}^{2}L_{\mathrm{b}}C_{\mathrm{b}}R_{0}}{R_{0}^{2}\left(L_{0}C_{0} - L_{\mathrm{b}}C_{\mathrm{b}}\right)^{2} + L_{0}^{2}L_{\mathrm{b}}C_{\mathrm{b}}} + R_{\mathrm{b}},\,\,(10)$$

$$\operatorname{Re}\left(Z(\omega=\omega_{\text{BDP}})\right) = \frac{2L_{\text{b}}^{2}L_{0}C_{0}R_{\text{b}}}{R_{\text{b}}^{2}(L_{\text{b}}C_{\text{b}}-L_{0}C_{0})^{2}+L_{\text{b}}^{2}L_{0}C_{0}} + 2R_{0}.$$
(11)

Figure 4(d) shows that R_b and R_0 , are, respectively, the dominant terms of $\operatorname{Re}(Z(\omega=\omega_{\text{CTP}}))$ and $\operatorname{Re}(Z(\omega=\omega_{\text{BDP}}))$. As w becomes wider, R_b increases and R_0 decreases (Fig. S11(e, f), Supplementary information), resulting to the strengthening of the CTP band and the weakening of the BDP band. In brief, the resonant frequencies and extinction intensities of both bands are strongly dependent on the nanobridge width which simultaneously determines the inductance and resistance of the nanobridge and the rhombic arms.

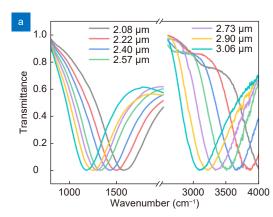
Tunability of MIR resonance and SEIRA

The resonant wavelengths of the two bands can be tuned not only by varying the width of nanobridge, but also by varying the total length l_0 of NBRAs (Fig. 5(a) and Fig. S14(a), Supplementary information), just as what is observed for the rods structures^{24–26}. The data between 2000~2600 cm⁻¹ is hided in Fig. 5(a) to highlight the resonant dips of both bands. Experimentally, the resonant wavelengths of the two bands, $\lambda_{\rm CTP}$ and $\lambda_{\rm BDP}$, redshift linearly as the length of NBRA l_0 increases with fitting functions $\lambda_{\rm CTP} = 2.14 \times l_0 + 1.93 \, (\mu {\rm m})$ for CTP band, and $\lambda_{\rm BDP} = 0.78 \times l_0 + 0.86 \, (\mu {\rm m})$ for BDP band (Fig. S14(b, c), Supplementary information). The tunability can be

further evidenced by antenna length-tuned Fano interference between molecular vibrational excitation and plasmon excitation^{24,63}. In our experiment, we functionalized a monolayer PNTP molecules whose symmetric stretching vibrational band of NO2 is centered at 1335 cm-1. As shown in Fig. 5(b), the lineshape of the band around 1335 cm⁻¹ of the measured SEIRA spectra evolves from an asymmetric Fano shape to a Lorentzian shape, and to an asymmetric Fano shape as the resonant wavenumber of the CTP band increases from 1176 cm-1 to 1496 cm⁻¹. For the BDP band covering the =C-H stretching band of PNTP at 3024 cm⁻¹, the SEIRA spectra around 3024 cm⁻¹ barely show a signal due to the weakness of the LFEF. Comparing with w, l_0 is less efficient when modifying the resonant wavelengths of the NBRA. As w increases 365 nm (from 5 nm to 370 nm), the resonant wavelengths of the CTP band and BDP band blue shift about 3.9 μ m and 0.45 μ m. However, as l_0 increases nearly 1 µm (from 2.08 µm to 3.06 µm), the resonant wavelengths of the CTP band and BDP band only red shift about 2.01 μm and 0.76 μm.

Nanogaped NBRA dimer

The spatially superimposed hotspots at the two extremities of the NBRA structure pave the way for further boosting up the local field for both bands in a NBRA dimer with a nanometer-size gap (nanogap). The NBRA dimer was fabricated with a ~20 nm gap size (see the SEM image and AFM topography in Fig. 6(a), 6(c) and Fig. S3(b), Supplementary information)). Other geometric parameters are the same as those of the structure in Fig. 1. The periodicities of the array are 6400 nm and 1000 nm along the long and short axes of the NBRA dimer, respectively. The normalized experimental transmittance spectra of NBRA dimers also exhibit two pro-



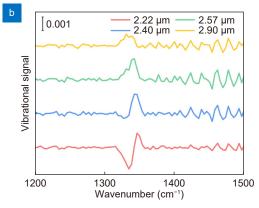


Fig. 5 | (a) Experimental transmittance spectra (normalized) as a function of the length of the NBRAs. (b) SEIRA spectra of PNTP on NBRAs with total lengths 2.22, 2.40, 2.57 and 2.90 µm in the range of the CTP band.

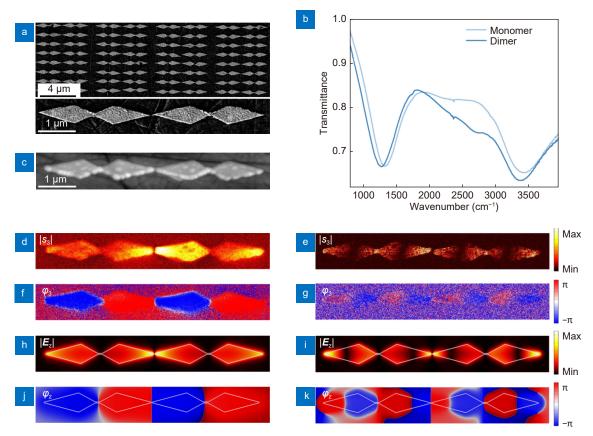


Fig. 6 | (a) SEM image of NBRA dimer. (b) Experimental transmittance of a NBRA and its dimer with gap size 20 nm. (c) AFM topography of a NBRA dimer. The scale bars in (a) and (c) are 1 μ m. Measured near-field amplitude (d) and phase (f) of NBRA dimer at 1100 cm⁻¹. Simulated mapping of $|E_z|$ (h) and φ_z (j) of NBRA dimer at 1100 cm⁻¹. Measured near-field amplitude (e) and phase (g) of NBRA dimer at 2100 cm⁻¹. Simulated mapping of $|E_z|$ (i) and φ_z (k) of NBRA dimer at 2100 cm⁻¹.

nounced resonance bands in MIR spectral range, one band centered at 1272 cm⁻¹ and the other one centered at 3367 cm⁻¹ (Fig. 6(b)). Both bands of NBRA dimer only redshift less than 100 cm⁻¹ in comparison with the monomer counterparts (Fig. 6(b)). To assign the plasmonic modes associated with the two bands, we employed the s-SNOM to measure the NBRA dimer for both bands. The near-field amplitude and phase images at 1100 cm⁻¹, as shown in Fig. 6(d) and 6(f), as well as the simulated $|E_z|$ and φ_z shown in Fig. 6(h) and 6(j), suggest that the band centered at 1272 cm⁻¹ is a gap-coupled CTP band of the NBRA-dimer structure. The near-field amplitude and phase images at 2100 cm⁻¹, as shown in Fig. 6(e) and 6(g), as well as the simulated $|E_z|$ and φ_z shown in Fig. 6(i) and 6(k), suggest that the band centered at 3367 cm⁻¹ can be assigned to a gap-coupled BDP band, although 2100 cm⁻¹ is located at the shoulder of the 3367 cm⁻¹ band. Notably, strong amplitude signals are found in the nanogap for both bands as expected^{47,64}. The simulated LEEFs at the hotspots of both bands in the NBRA dimer are 6.3 and 5.0 times larger than those of the NBRA monomer. Further shrinking the nanogap size from 20 nm to 5 nm, the LFEF can be boosted up about 20 times. Moreover, the logarithm of the EFs linearly depends on the gap size with the slope about -2 for both CTP and BDP bands (Fig. S16, Supplementary information), indicating that the near-field coupling through the nanogap for both bands in the NBRA dimer is attributed to the capacitive coupling²⁸.

NBRA dimer-waveguide-cavity coupling

To further enhance LFEFs for both bands, we adopted a strategy by the optical coupling between a localized surface plasmon (LSP) mode and a waveguide-cavity mode^{14,65-67}. As shown in Fig. 7(a), a NBRA dimer was fabricated on a reflective substrate (the NBRA dimer-on-reflector structure). The reflective substrate was prepared by depositing 3 nm of Ti and 200 nm of Au onto a Si wafer using electron beam evaporation followed by depositing 3 nm of Al and 1400 nm of SiO₂ using vacuum magnetron sputtering. Previous studies focused on a single LSP mode coupled with the waveguide cavity

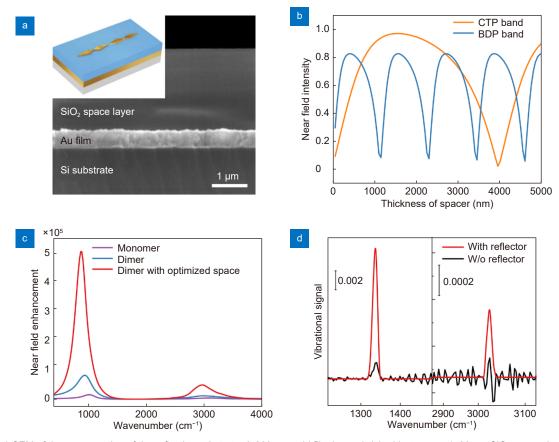


Fig. 7 | (a) SEM of the cross section of the reflective substrate. A 200 nm gold film is sandwiched between a 1400 nm SiO_2 spacer layer and the Si substrate. The scale bar is 1 μ m. Inset: schematic of the NBRA dimer-on-reflector structure to integrate the waveguide-cavity coupling and nanogap coupling. (b) Normalized LFEFs of CTP mode (blue curve) and BDP mode (orange curve) as a function of the thickness of the spacer layer. (c) Simulated LFEFs of monomer, dimer and dimer with 1400 nm SiO_2 spacer layer. (d) SEIRA spectra of PNTP on NBRA dimer on transmitted substrate or on reflective substrate.

mode^{14,67}. In this study, we are targeting at both gapcoupled CTP and BDP bands rather than only one band of the NBRA that can be simultaneously and constructively coupled with the respective waveguide cavity modes on the same reflective substrate.

We numerically optimized the thickness of the spacer layer to simultaneously maximize the LFEFs in the nanogap of the NBRA dimer for both bands. Figure 7(b) shows that the simulated normalized LFEFs in the nanogap of the NBRA dimer-on-reflector structure for the gap-coupled CTP and BDP bands fluctuate periodically as the thickness of spacer layer (SiO₂) increases, with periodicities 4800 nm and 1150 nm, respectively. The periodical behavior can be also predicted through the basic principles for electromagnetic waves⁶⁸. We found that 1400 nm was the thinnest thickness of the SiO₂ layer for almost simultaneously maximizing LFEFs in the nanogap of the NBRA dimer-on-reflector structure with additional 6.6 times and 4.0 times for the gap-coupled CTP and BDP bands, respectively (Fig. 7(c)), in compar-

ison with those of the NBRA dimer without the reflector. Integrally, the LFEFs in the nanogap of the NBRA dimeron-reflector structure of both bands will be enhanced by 36.75 times and 12.35 times for CTP and BDP bands, respectively, compared with the NBRA monomer through nanogap coupling and waveguide-cavity coupling (Fig. 7(c)).

Experimentally, the SEIRA spectra of a monolayer of PNTP molecules on the surface of the NBRA dimer with or without the reflector structure (thickness of SiO₂ spacer layer, 1400 nm) further demonstrate the additional enhancement for both bands through waveguide-cavity coupling (Fig. 7(d)). The integral absorption intensities around 1335 cm⁻¹ and 3024 cm⁻¹ bands for the NBRA dimer-on-reflector structure are 7.4 times and 6.9 times larger than those of NBRA dimer without the reflector. The experimental results show that it is a practical strategy to boost the LFEFs associated with both bands by the waveguide-cavity coupling.

Conclusions

In summary, we have reported a nanobridged rhombic structure as a new type of MIRA, effectively exciting the high-order mode (BDP mode) and the fundamental mode (CTP mode) through charge transfer plasmon, which has been demonstrated by the s-SNOM measurements. The RLC circuit analysis reveals that the nanobridge and the linked rhombic-arm antennas mainly act as the inductance and resistance of the overall structure and determines the resonant frequency and intensity of the high-order mode, as well as those of the fundamental band. The hotspots associated with both bands are spatially superimposed, enabling further boosting up the LFEFs of both bands in a NBRA dimer with a nanogap. Integrating waveguide-cavity coupling, the LFEFs in the nanogap of NBRA dimer-on-reflector structure associated with both bands can be simultaneously improved by up to one order of magnitude in contrast to the NBRA monomer counterpart, thereby achieving monolayer sensitivity for two fingerprints.

We provide a new approach for designing multiband antenna by charge transfer plasmon, efficiently exciting the high-order modes, along with elaborating the importance of the nanobridge and nanogap in MIRAs. These findings also indicate that the island-like metallic films developed as the SEIRA-active substrates in the early stage of SEIRA in 1980s could be considered as nanogap-coupled MIRAs with nanobridges⁶⁹. We believe that designing novel structures with nanobridges accompanied with nanogaps can be a promising strategy for producing multiband MIRAs for general applications in SEIRA, heat-management, and ultrasensitive MIR detectors in the future.

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Author contributions

S. Y. Ding conceived the idea. E. M. You and J. Yi performed the simulations. Y. Q. Chen and H. G. Duan fabricated the structures and measured the SEM of the NBRA structure. E. M. You performed the micro-FTIR and s-SNOM measurements. E. M. You and Z. D. Meng performed the RLC circuit modelling. Q. Chen and E. M. You measured the SEM of the cross section of the reflective substrate. S. Y. Ding and H. G. Duan supervised the project. E. M. You, Y. Q. Chen, J. Yi, S. Y. Ding, H. G. Duan, M. Moskovits and Z. Q. Tian contributed to the writing of the manuscript.

Competing interests

The authors declare no competing financial interests.

Supplementary information

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