Recent improvement of silicon absorption in opto-electric devices
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Silicon dominates the contemporary electronic industry. However, being an indirect band-gap material, it is a poor absorber of light, which decreases the efficiency of Si-based photodetectors and photovoltaic devices. This review highlights recent studies performed towards improving the optical absorption of Si. A summary of recent theoretical approaches based on the first principle calculation has been provided. It is followed by an overview of recent experimental approaches including scattering, plasmon, hot electron, and near-field effects. The article concludes with a perspective on the future research direction of Si-based photodetectors and photovoltaic devices.

Keywords: Si; indirect band gap; plasmon; first principle calculation; near-field effect

Introduction

Si is an integral part of all electronic devices. It plays an important role in opto-electronic devices such as photodetectors and photovoltaic devices\(^1\). However, since it is an indirect band-gap material, phonon assistance is required in the photo-excitation process to compensate the wave-vector difference between the valence band maximum and the conduction band minimum of holes (Γ point) and electrons (X point), respectively (Fig. 1\(^1\)). Therefore, although Si dominates the photonics devices, a field that is better known as Si photonics\(^1\), it is a substrate for the light emitting materials\(^5,6\). Moreover, it can be used for a much wider variety of applications if its optical absorption in the telecommunication wavelength range is improved\(^7\). In this article, some important recent studies directed towards improving the performance of Si photonic devices have been reviewed.

Theoretical advances

Optical near-field (ONF) effect can potentially improve the carrier excitation in indirect band-gap materials. This is attributed to the fact that ONF is expected to have large wave vector components (Δk), which implies very small Δx, due to the field localization. This was validated in a study which demonstrated that ONFs, as a dipole-mode plasmon, generate carriers directly\(^6\). It was shown that in small particles, the plasmons induce an electric field that exhibits Fourier components with large wave numbers. Furthermore, it was demonstrated that such an electric field generates carriers without phonon assistance. Further investigation of the ONF excitation was performed

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Fig. 1 | Comparison of far- and near-field excitations. (a) Far-field (FF) excitation of Si. Here \(k_{\text{photon}}\), \(k_c\), \(k_v\), and \(k_{\text{phonon}}\) are the wave vectors of photon, conduction band, valence band, and phonon, respectively. (b) Optical near-field (ONF) excitation of Si. Figure is reproduced from ref.\(^1\) under the terms of the Creative Commons Attribution 4.0 International license.
in a system comprising of metallic nanospheres embedded in crystalline Si. Here, the excitation was evaluated under the framework of linear perturbation theory, and it was found that the ONF effect is too weak to be measured in a real system. However, these calculations were based on analytical model systems, and not on the real carrier excitations.

To this end, Yamaguchi et al. evaluated the carrier dynamics using first-principles calculations, where they calculated the electron excitation by considering the indirect interband transition between states with different Bloch wave numbers. Instead of using the Bloch condition, which cannot describe the indirect interband transitions, they implemented the Born-von Kármán boundary condition. Further, they also performed a time-dependent calculation of the ONF excitation using one-dimensional Kronig-Penny (1D-KP) model (Figs. 2(a) and 2(b)). They considered the dispersion relation with an indirect band gap (Fig. 2(c)). As shown in Figs. 2(d) and 2(e), it was observed that the absorption spectra for far-field excitation decreases at the band-gap energy ($E_g$), while the absorption spectrum for near-field excitation decreases at the band-gap energy ($E_p$) (much smaller than $E_g$) which was realized by the direct excitation. Furthermore, they clearly showed that the near-field component of the dipole radiation ($r^3$) is the origin of ONF excitation.

A more detailed investigation of the ONF excitation in realistic three dimensional Si systems (Fig. 3(a)) was reported recently. Here, a real-time and real-space grid-based time-dependent density-functional theory (DFT) approach was used. A supercell method along with the Born-von Kármán periodic condition was implemented to calculate the wave-vector excitation, where the vertical band gap energy at the $\Gamma$ point was 2.0 eV. In this system, the source of the ONF was a $y$-polarized point dipole with the near-field component ($r^3$), which was set 5 Å apart from the surface of Si. Thus, realistic metallic structures, which could generate plasmon, were not treated explicitly in this study. The potentials of the ONF were described by

$$V_{\text{near}}(r,t) = -\frac{C(y-y_p)}{r^3} \sin(\omega t) \sin^2\left(\frac{\pi t}{T}\right),$$

where $\omega$ is the frequency of the oscillating dipole, $C$ is a constant, and $T = 30$ fs is the pulse duration. The electric field distribution induced by the oscillating dipole, as described by Eq. (1) is non-uniform in spatial domain (see Fig. 3(b)). Therefore, it results in the generation of large components of the Fourier domain as shown in Fig. 3(c), which implies that the ONF has large wave vectors. Based on these observations, the absorption intensity was obtained by calculating the transition probability. As shown in Fig. 3(d), the absorption intensity for the far-field excitation (blue solids circles and blue line) decreases around 2.0 eV, which corresponds to the band gap energy at the $\Gamma$ point. On the contrary, the ONF induces a sufficiently large absorption intensity, which causes a red shift of the absorption spectra (red solid circles and red line in Fig. 3(d)). Furthermore, direct optical transitions between different wave vectors were also confirmed. Figure 3(e) shows the absorption intensity as a function of the variation in wave vector for the electronic excitation between second-highest valence band and the lowest conduction band in the ONF excitation at 1.6 eV. Here, the absorption intensity is maximum at $\Delta k \sim 4$ nm$^{-1}$.

**Fig. 2 | ONF excitation in indirect band-gap structure.** (a) Potential, (b) a schematic of the 1D-KP model, and (c) dispersion relation. Here, $E_s$: band-gap energy and $E_p$: direct band-gap energy. Frames (d) and (e) show the normalized absorption spectra of the 1D-KP model due to the far- and near-field excitations, respectively. (f) Absorption spectra due to the electric field components from the dipole radiation, which are $r^3$ (red solid line), $r^4$ (blue dashed line), and $r^5$ (green dotted line). Figure is reprinted with permission from ref.10. Copyright © 2016 American Physical Society.
This was the direct evidence of the wave-vector excitation induced by the ONF. In other words, the direct ONF excitation does not require phonon assistance and can be realized with photons exclusively.

**Experimental advances**

**Scattering effect: Black Si**

A simple yet effective way to improve the optical absorption in the solar cells is to increase the optical path length through the depletion layer between the p-n junction. To improve the light scattering efficiency, the scatterers have been fabricated at the surface of the detector, such as pyramidal Si hillocks made by the anisotropic etching, or needles made by the laser irradiation with the ultra-short pulse width. In particular, the latter (Si surface with needles) works as an extremely good scatterer because of a high coupling efficiency can be realized by controlling the size and the shape of the metallic nanoparticle. In particular, it was observed that smaller size, as well as cylindrical and hemispherical shapes of spheres lead to a longer path length in the substrate. Further improvement of the carrier-excitation was realized by introducing a photonic design to induce light trapping with three-dimensional structures consisting of nanowires and nanoparticles.

**Plasmonic effect**

To improve the scattering efficiency, many researchers utilized the field enhancement using the plasmon resonance. The scattering and absorption cross-sections are given by point dipole model:

\[
C_{\text{sc}} = \frac{k^4}{6\pi|\alpha|^2} \frac{8\pi}{3\lambda} a^3 \left( \frac{\varepsilon - \varepsilon_m}{\varepsilon + 2\varepsilon_m} \right)^2, \tag{2}
\]

where \(\alpha\) is the polarizability, \(a\) is the radius of the particle, \(\varepsilon\) is the dielectric function of the particle, \(\varepsilon_m\) is the dielectric function of the surrounding media, and \(\lambda\) is the wavelength. It is evident from Eq. (2) that \(\varepsilon\) should be negative (\(-2\varepsilon_m\)), i.e., the scatterer should be a metal, to utilize the plasmon resonance for the light scattering. Further from Eq. (3), it is clear that the plasmon induced light scattering is indispensable for a strong optical absorption. For a more effective trapping of the scattered light at the metallic nanoparticles on the surface, the scattered light excites the waveguide mode using a thin Si substrate of Si-on-insulator (SOI) wafer. Furthermore, a higher coupling efficiency can be realized by controlling the size and the shape of the metallic nanoparticle. In particular, it was observed that smaller size, as well as cylindrical and hemispherical shapes of spheres lead to a longer path length in the substrate. Further improvement of the carrier-excitation was realized by introducing a photonic design to induce light trapping with three-dimensional structures consisting of nanowires and nanoparticles. Since the plasmon resonance for the Au sphere occurs at ~520 nm, ellipsoid shape, chains of nanoparticles, or elongated shapes such as nanorod with longer resonance wavelength have been implemented to obtain larger absorbance in this wavelength range. In addition, the periodic structure of the metal, i.e., metamaterial-plasmonic absorbers, has been investigated to enhance the optical absorption. The periodic
structure works as a grating coupler of light with a normal incident angle. Consequently, it results in a strong absorption exceeding 80%. We investigated the self-assembly method\textsuperscript{35} to improve the efficiency of nanoparticles deposition. Using the laser-assisted deposition of the electrode metal with a reverse biased p–n junction, we realized a selective photocurrent generation in the transparent wavelength range\textsuperscript{38}. We observed a drastic change in the surface morphology of the metal, and confirmed the increase in the photocurrent at the wavelength that is close to that used during the electrode deposition. Since Au has high absorption coefficient, alternative materials, such as transparent conducting oxides were considered to achieve the resonance at longer wavelengths\textsuperscript{39,40}.

**Hot electrons**

The internal photoemission on a Schottky barrier (Fig. 4) has been investigated to utilize the scenarios where the photon energy is lower than the band gap energy of Si ($E_c−E_V=1.1$ eV)\textsuperscript{41–43}. Since the Schottky barrier between Au and Si ($\phi_B−0.5$ eV) is lower than the band gap energy of Si, the infrared wavelength region that is longer than the band-gap wavelength (1100 nm) can be used. The carriers of electron (hot electrons) were excited to obtain energies that are higher than the Schottky barrier. By optimizing the plasmon resonator, the responsivity of 4.5×10\textsuperscript{-4} A W\textsuperscript{-1} was obtained at nearly 1600 nm (~0.77 eV). Using a three dimensional plasmonic resonator, a photocapacitance structure was developed to detect the charge generation at the Schottky barrier with higher efficiency (Fig. 4(b))\textsuperscript{44}.

**Near-field effect**

As discussed in the previous section, the ONF effect can improve the absorption efficiency at the band-gap wavelength. This implies that the localized field can induce large wave vector components, which in turn leads to direct excitation in indirect band-gap semiconductors (Fig. 1(b)). To corroborate this effect, we fabricated a Si photodetector with a lateral p–n junction (Fig. 5(a))\textsuperscript{4}. We avoided the field enhancement due to the Au nanoparticles\textsuperscript{24,26,27} in this device by introducing their near-field sources with extremely low coverage ~2 % (Figs. 5(b) and 5(c)). Consequently, we observed a 40 % increase in the photosensitivity as compared to that without Au nanoparticles (Figs. 5(d) and 5(e)). As shown in Fig. 5(e), the photosensitivity rate increased at longer wavelengths near the band-gap wavelength. This dependence has not been reported for devices that utilized plasmon resonance\textsuperscript{23,24,26,27}, where the enhancement in photosensitivity exhibits a peak around the plasmon resonance, which is determined by the materials and shapes. To find the origin of this dependence, we evaluated the wavelength dependence under the assumption that the ONF effect causes a direct excitation in the indirect band-gap semiconductor. The absorption coefficients of the indirect ($\alpha_i$) and the direct ($\alpha_d$) band-gap materials near the energy band gap $E_g$ are described as\textsuperscript{45}

$$\alpha_i \propto (h\nu−E_g)^{3/2} / h\nu , \quad (4)$$

$$\alpha_d \propto (h\nu−E_g)^{1/2} / h\nu , \quad (5)$$

where $h$ is Planck constant and $\nu$ is frequency of light. Since the bias voltage was 0, the photo-current becomes the short circuit current described as\textsuperscript{46}

$$I_{sc} = Q(1−R)[1−\exp(−\alpha l)]en , \quad (6)$$

where $Q$ is the collection efficiency, $R$ is the reflection coefficient, $l$ is the absorbing layer thickness, $e$ is the electron charge, and $n$ is the number of photons per second per unit of the p–n junction. The ONF can induce a direct transition by the inclusion of Au nanoparticles. Thus, the photocurrent for this device is the same as that of the direct transition ($I_{sc}D$). However, since the coverage of the Au nanoparticles $A$ is not 100 %, the photocurrent shows an increase in the regions where Au nanoparticles existed (the ratio was $A$), while it remained the same (the ratio was $(1−A)$) in other regions. Thus, the increased rate in the device can be expressed as follows:

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where $C$ is the proportional constant. As shown in Fig. S(e), the solid curves represent the calculated increased rates, where blue, red, and black curves correspond to $N = 10$, $5$, and $1$, respectively. The experimental data confirmed that the observation of increased rate near the band-gap energy supports the possibility of the direct transition by the ONF. Further improvement of the increased rate can be realized by implementing a larger coverage of the Au nanoparticles and a larger depletion area by introducing the intrinsic Si layer between the p- and n-type layers, i.e., p–i–n diode structure.

Figure 6(a) shows the variation of increased rate as a function of size of the Au nanoparticles. We observe that the increased rate is maximum for Au nanoparticle with a diameter of 100 nm. To quantify this size dependence, numerical calculations were performed using a finite difference time domain (FDTD) method\cite{ref19}. The calculated field distributions (Fig. 6(b)) were then used to obtain the Fourier spectra (Fig. 6(c)), where the spectra were obtained from the cross-sectional profile of the field distribution along the $x$-axis and they were averaged along $y$-axis $0 \leq y \leq D/2$ ($D$ is the diameter of Au nanoparticle).

Since the wave number difference between the $\Gamma$ and $X$ points ($k_{\Gamma X}$) is 4.92 nm$^{-1}$\cite{ref20}, we studied the diameter dependence of the power spectrum at $k_{\Gamma X}$ ($\left|F(E)_{\Gamma X}\right|^2$, red circles in Fig. 6(d)). It is observed that $F(E)_{\Gamma X}$ also attains a maximum at $D = 100$ nm. The calculated size dependence is found to be in good agreement with the experimental results (Fig. 6(a)). The effect of generating a larger $k$-component by the ONF was then investigated by determining the normalized power spectra. This normalization was performed using the square of the volume of Au nanoparticles (open blue circles in Fig. 6(d))\cite{ref21}. The normalized power spectra increase with a decrease in size. These calculations confirm that, a greater $\Delta k$ is generated when the size of Au nanoparticles decreases. In other words, the efficiency of the direct optical transition by the ONF increases with a decrease in size due to large components of the wave number.
Although the theoretical results of the large $\Delta k$ generated using the first-principle calculation\(^{14}\) supported the experimental results\(^{1}\) qualitatively, the enhancement value was not explained quantitatively. The disagreement might be due to the disagreement of the materials and the size. For example, in the first-principle calculation, the point dipole was used as a source of the ONF. More detailed calculations using the real material in a real system will be required to discuss quantitatively. In addition, the limitation of the material size in the first-principle calculation results in the disagreement of the system size. To resolve this disagreement, a smaller size of the source for ONF generation should be used, such as porous Si with several nanometer scale\(^{50-52}\).

**Summary and future directions**

Si is an indirect band-gap semiconductor and therefore exhibits poor optical absorption efficiency. This review presents an overview of various theoretical and experimental efforts to improve the performance of Si-based photodetectors and photovoltaic devices. The theoretical framework based on first principle calculations along with experiments including scattering effect, plasmon effect, hot electrons, and near-field effect were discussed. The ONF effect permits the generation of a large $\Delta k$ by field localization, which in turn can improve the absorption efficiency of these devices. The ONF effect can intrinsically induce a direct transition due to nonuniformity of the optical field. In addition to the reviewed topics, we confirmed that near-field could enhance the optical absorption by the field enhancement effect\(^{13}\), which does not utilize plasmon resonance. The field enhancement by ONF was confirmed both in the first-principle calculation and in the experimental absorption spectra of the metal complex for CO\(_2\) reduction. Therefore, if the near-field source is placed with appropriate position, further enhancement of absorption is expected. Further, since the ONF has nonuniform optical field distribution in nanoscale, the ONF can generate even harmonics in materials with inversion symmetry\(^{34}\). Yamaguchi et al. have showed that the ONF inherently realizes strong second harmonic generation (SHG) and suggested ways to improve the efficiency of this process\(^{36,55-57}\). Further improvements of Si-based opto-electronic devices may be achieved by combining and optimizing these effects. Recently, the band engineering method was proposed to enhance the absorption in another indirect band-gap material (Ge)\(^{35}\). Similar investigations have been made in other indirect band-gap materials including InSe\(^{59-61}\) and MoS\(_2\)\(^{62,63}\). The enhancement was achieved by introducing

![Fig. 6](image-url) | Increased rate as a function of the size of Au nanoparticles. (a) Increased photosensitivity rate at a wavelength of 1100 nm versus diameter of the Au nanoparticles. (b) Electric-field intensity distribution $E^2$ at the interface of Au nanoparticle (diameter $D=100$ nm). (c) Averaged (0 ≤y≤2D/2) Fourier spectra along $x$-axis of the electric-field. The wave number difference between the $Γ$ and $X$ points: $k_{ΓX}=4.92$ nm\(^{-1}\). (d) Red solid circles: the diameter dependence of the power spectra at $k_{ΓX}=4.92$ (nm\(^{-1}\)), $|\langle E \rangle_{ΓX}^2|$. Blue open circles: the normalized value of the $|\langle E \rangle_{ΓX}^2|$ by the square of the volume, $|\langle E \rangle_{ΓX}^2|/r^2$. Figure is reproduced from ref.\(^{1}\) under the terms of the Creative Commons Attribution 4.0 International license.
a strain in the crystal, which changed the band diagram to the direct band-gap structure. Overall, indirect bandgap materials open new avenues for various applications, which are not limited to photodetectors\textsuperscript{1,2,6,66} and photovoltaic devices\textsuperscript{1,2}, but also include other realms such as light-emitting devices\textsuperscript{67,68}, water-splitting\textsuperscript{62,69}, etc.

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Competing interests

The author declares no competing financial interests.